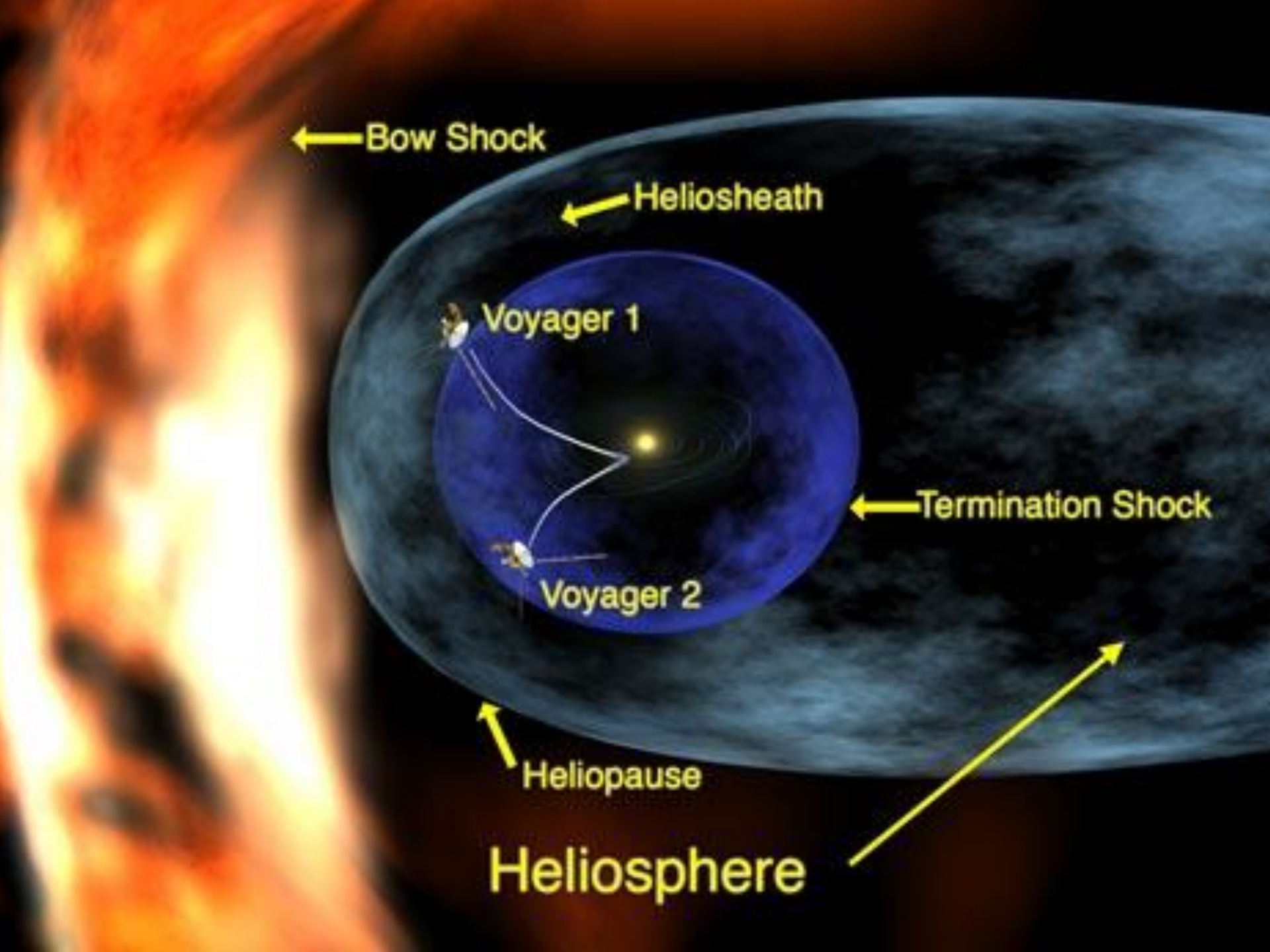


# *Last time...*

- Comments on homework
  - Double epsilons
  - integrals
- Space weather stories
- CMEs

# *Lecture 36*

- Solar wind turbulence
  - Energy spectrum
  - Dimensional analysis
- Heliosphere & termination shock
- Voyager 1 + 2
  - Messages to us & from us
  - Magnetic fields of planets



← Bow Shock

← Heliosheath

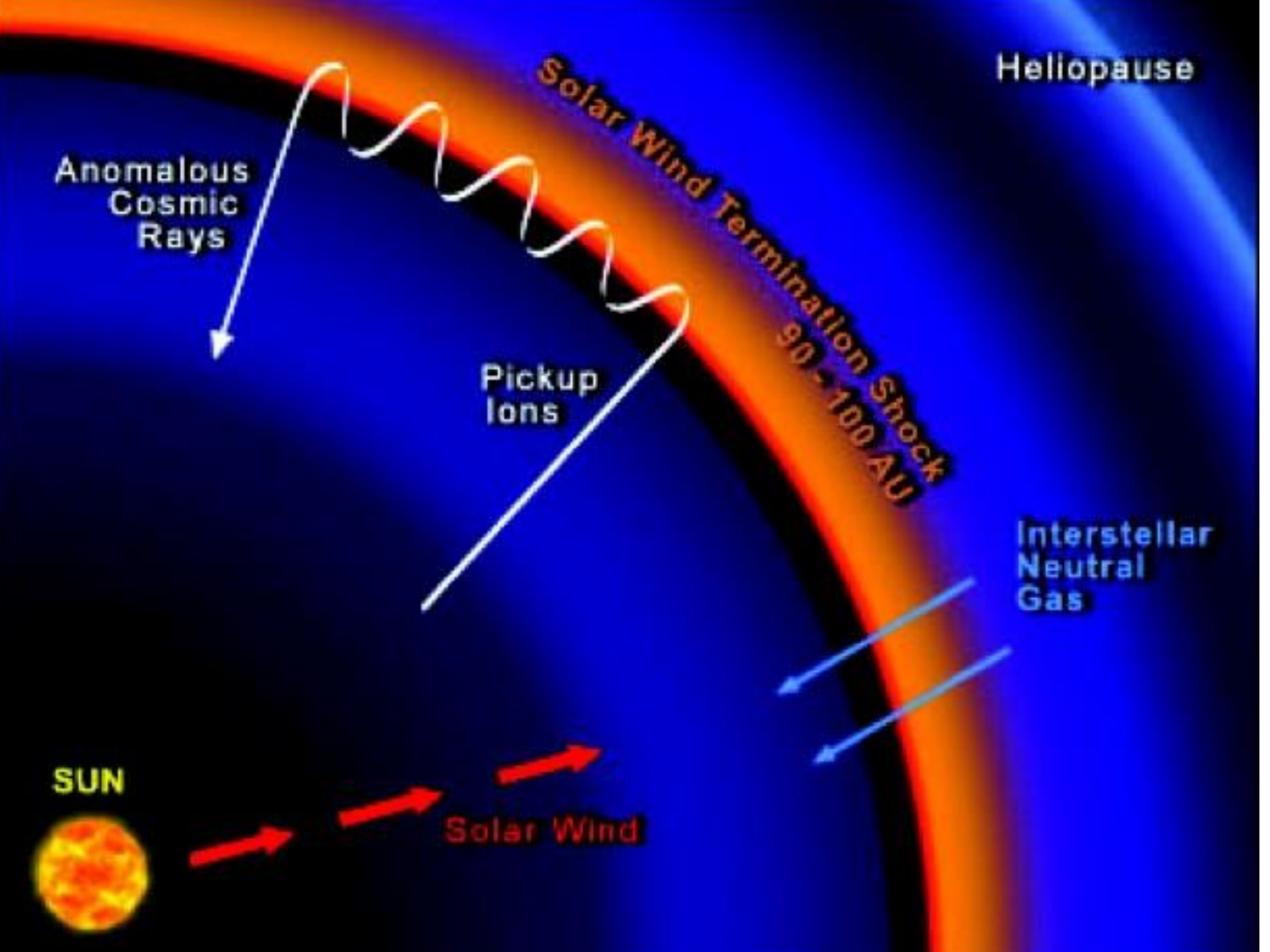
Voyager 1

Voyager 2

← Termination Shock

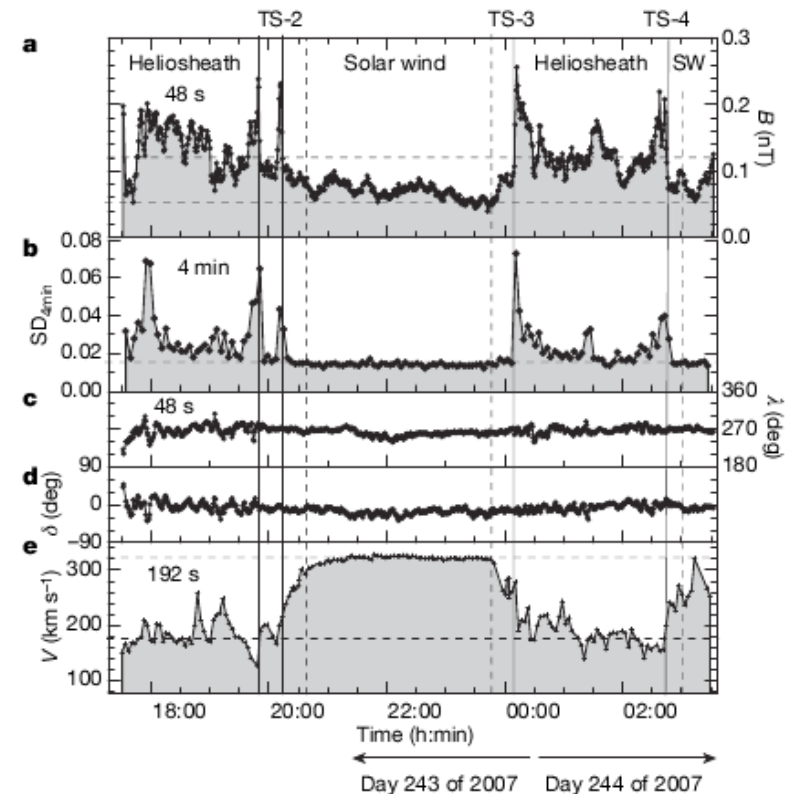
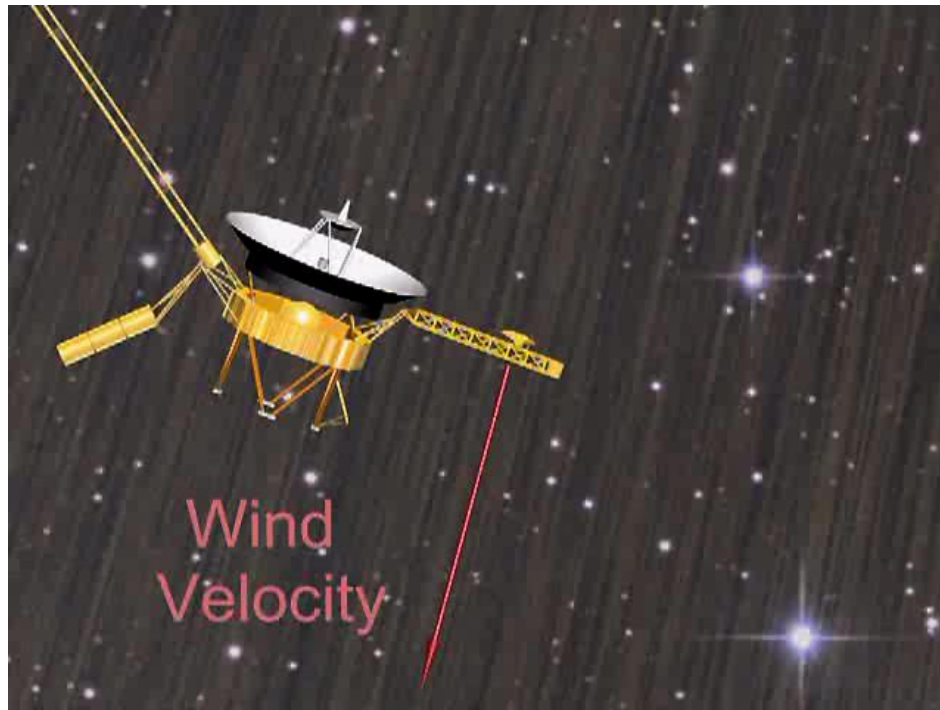
← Heliopause

Heliosphere



# Magnetic fields at the solar wind termination shock

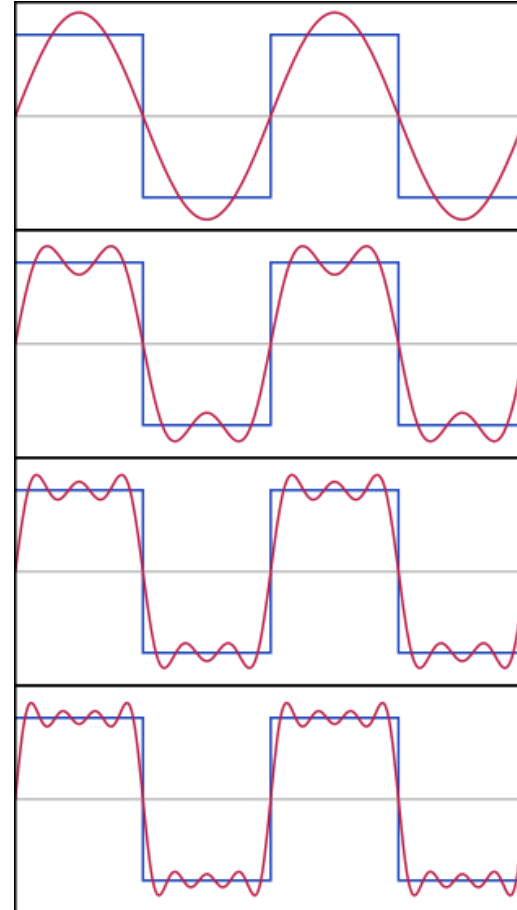
L. F. Burlaga<sup>1</sup>, N. F. Ness<sup>2</sup>, M. H. Acuña<sup>1</sup>, R. P. Lepping<sup>1</sup>, J. E. P. Connerney<sup>1</sup> & J. D. Richardson<sup>3</sup>



# *Lect. 12: could you explain Fourier analysis?*

- A. Yes
- B. Maybe
- C. Probably not
- D. Certainly not

$$f(t) = \sum_{n=1}^{\infty} a_n \underbrace{\sin(2\pi n / P) t}_{\omega_n}$$



# Lect. 13

$$\Delta\omega = \frac{2\pi}{t_{\max}} \quad \omega_{\max} \stackrel{?}{=} \frac{2\pi}{\Delta t} \quad \omega_{\text{Nyquist}} = \frac{\pi}{\Delta t}$$

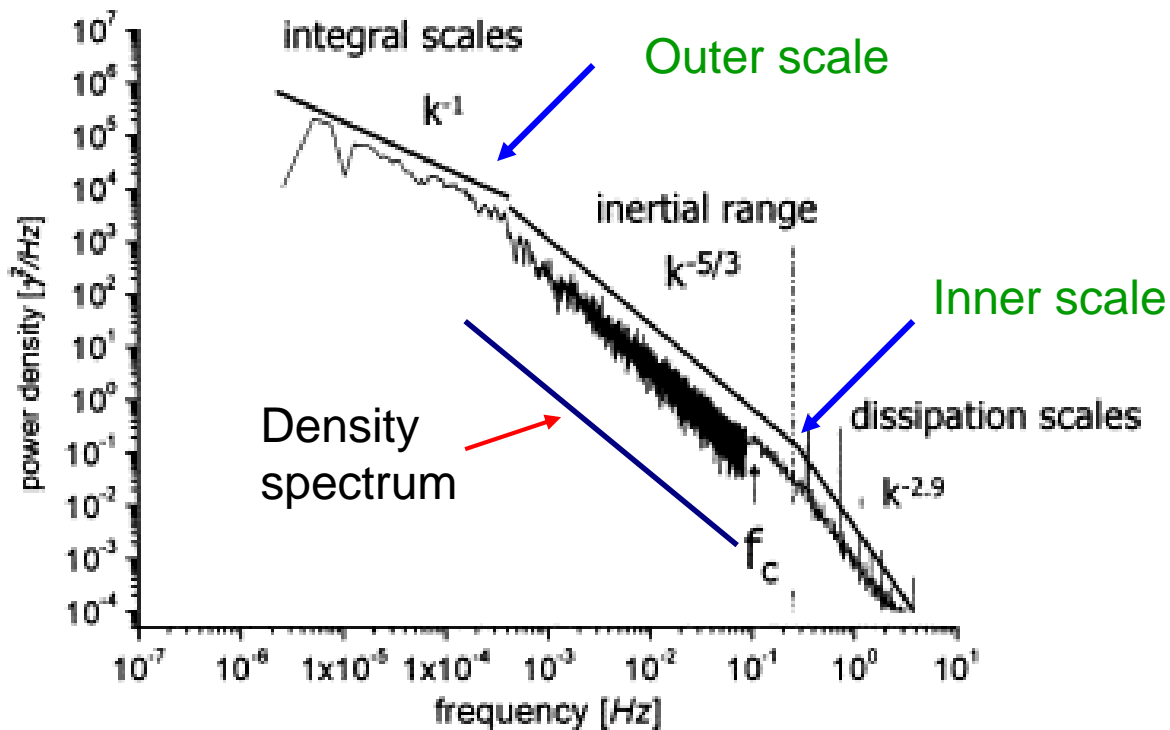
Because there are also  
negative frequencies

$$-\omega_{\text{Nyquist}} \leq \omega \leq \omega_{\text{Nyquist}} - \Delta\omega$$

- Small wavenumbers  $\rightarrow$  large scales
- Large wavenumbers  $\rightarrow$  small scales

# Turbulence spectra measured directly in the solar wind

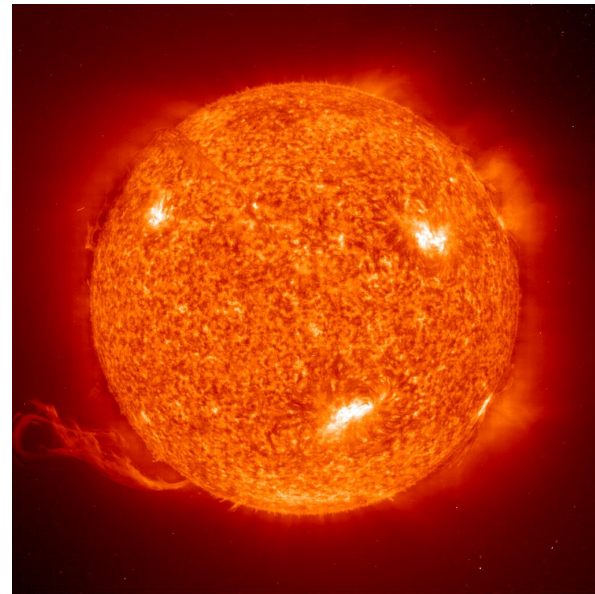
Magnetic  
power  
spectrum



R. Bruno, B. Bavassano, Ad Sp. Res. 35, 939, 2005



turba → confusion, crowd



# Da Vinci's conceptions



Large eddies → smaller eddies

# Sentimental comments on turbulence

- **Werner Heisenberg** was asked what he would ask God, given the opportunity. His reply was: "When I meet God, I am going to ask him two questions: Why **relativity**? And why **turbulence**? I really believe he will have an answer for the first."
- **Horace Lamb**—his choice being quantum mechanics (instead of relativity) and turbulence. Lamb was quoted as saying in a speech to the British Association for the Advancement of Science, "I am an old man now, and when I die and go to heaven there are two matters on which I hope for enlightenment. One is **quantum electrodynamics**, and the other is the **turbulent motion of fluids**. And about the former I am rather optimistic."<sup>[3]</sup>

# Hydrodynamic Equations

$$m \frac{d\mathbf{u}}{dt} = \mathbf{F}$$

Newton's equation

$$\rho \frac{D\mathbf{u}}{Dt} = -\nabla p + \mathbf{f} + \mu \nabla^2 \mathbf{u}$$


Navier-Stokes equation

$$\mathbf{u} = \mathbf{u}(t, \mathbf{x}) \quad \text{chain rule}$$

Reynolds number

$$\begin{aligned} \frac{D\mathbf{u}}{Dt} &= \frac{\partial \mathbf{u}}{\partial t} + \frac{\partial x_j}{\partial t} \frac{\partial \mathbf{u}}{\partial x_j} \\ &= \frac{\partial \mathbf{u}}{\partial t} + \mathbf{u} \cdot \nabla \mathbf{u} \end{aligned}$$

$$\frac{|\mathbf{u} \cdot \nabla \mathbf{u}|}{|\nu \nabla^2 \mathbf{u}|} \sim \frac{ul}{\nu} \equiv \text{Re}$$


$$\nu = \mu / \rho$$

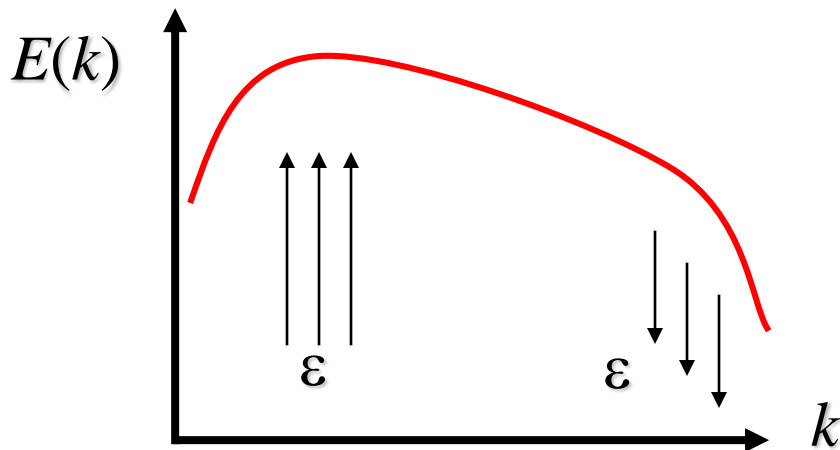
# Kolmogorov spectrum

nonlinearity

$$(\cos kx)^2 = \frac{1}{2} \cos 2kx + \frac{1}{2}$$

$$k \rightarrow 2k$$

constant flux  $\varepsilon$  [ $\text{cm}^2/\text{s}^3$ ]



$$\int E(k) dk = \frac{1}{2} \langle \mathbf{u}^2 \rangle \quad [\text{cm}^3/\text{s}^2]$$

$$E(k) = C_K \varepsilon^a k^b$$

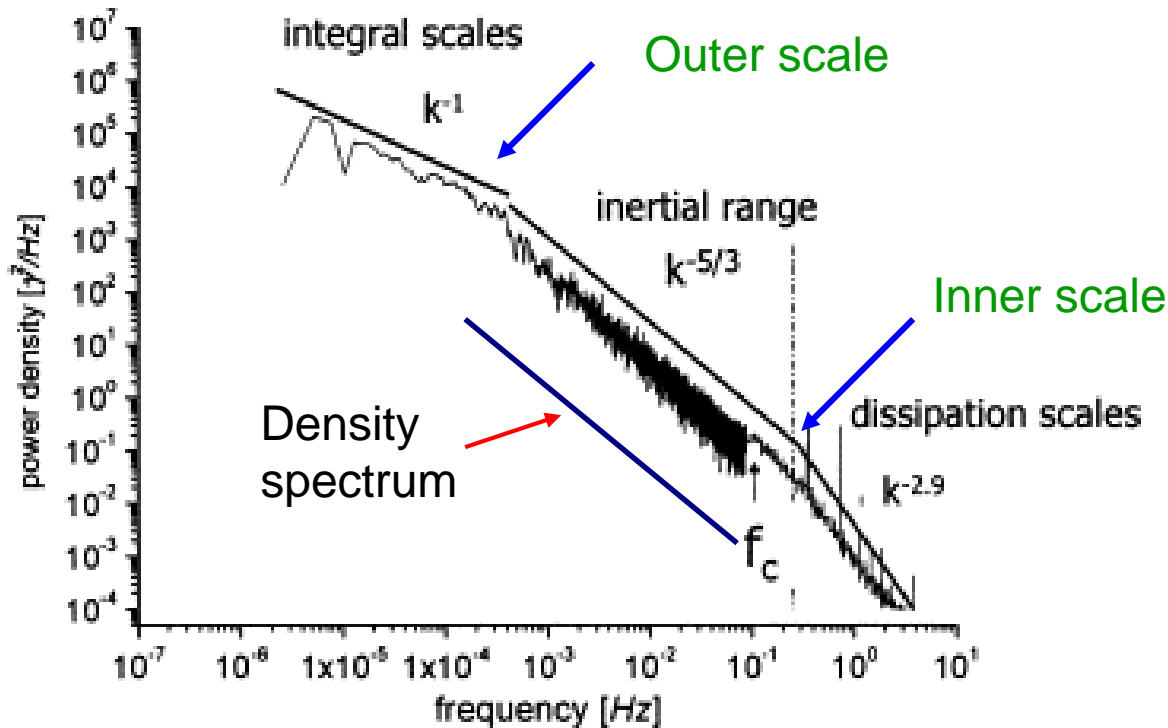
$$\text{cm: } 3 = 2a - 1$$

$$\text{s: } 2 = 3a$$

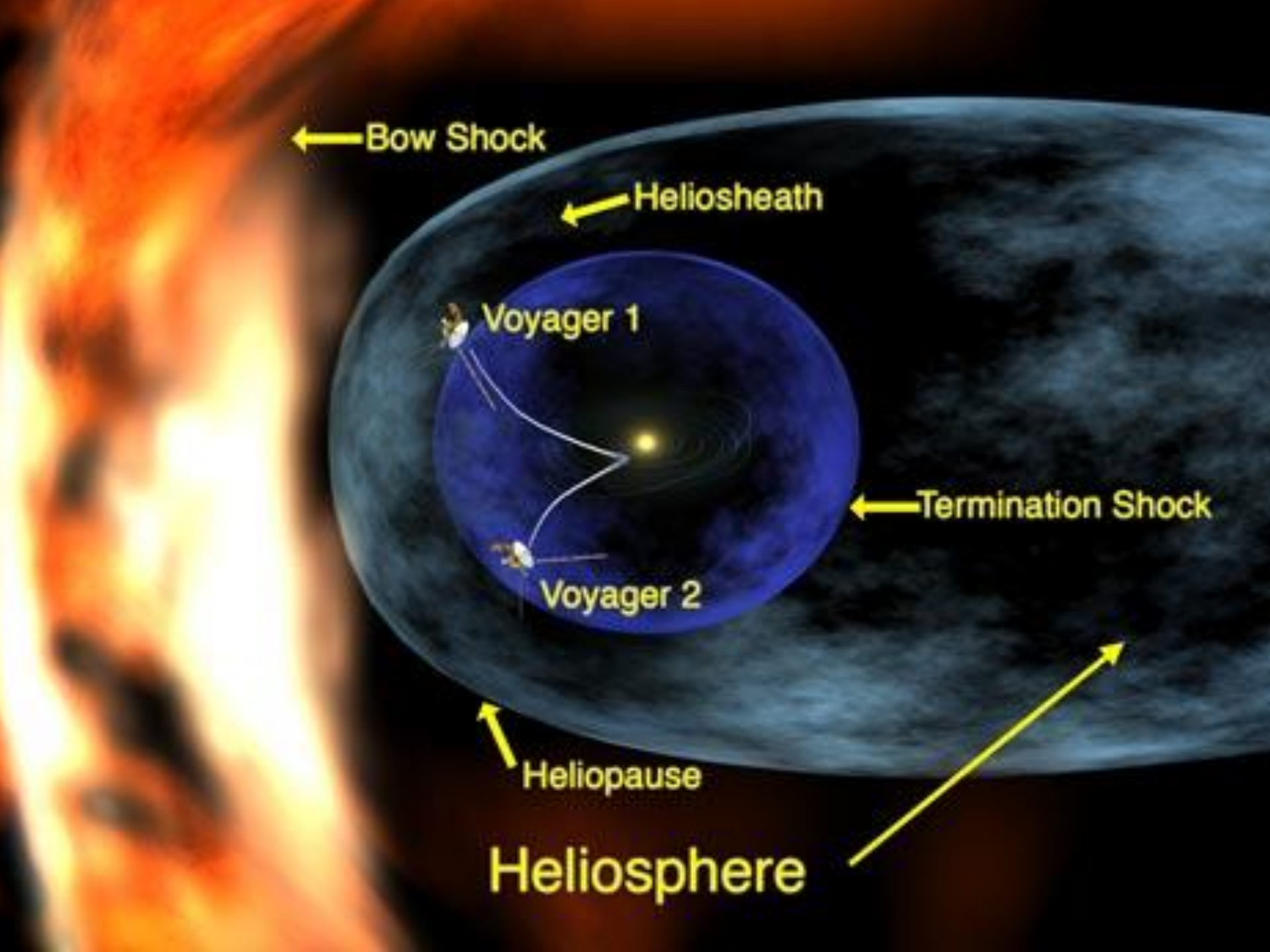
$$a = 2/3, \quad b = -5/3$$

# Turbulent spectra can be measured directly in the solar wind

Magnetic  
power  
spectrum



R. Bruno, B. Bavassano, *Ad Sp. Res.*  
35, 939, 2005



← Bow Shock

← Heliosheath

Voyager 1

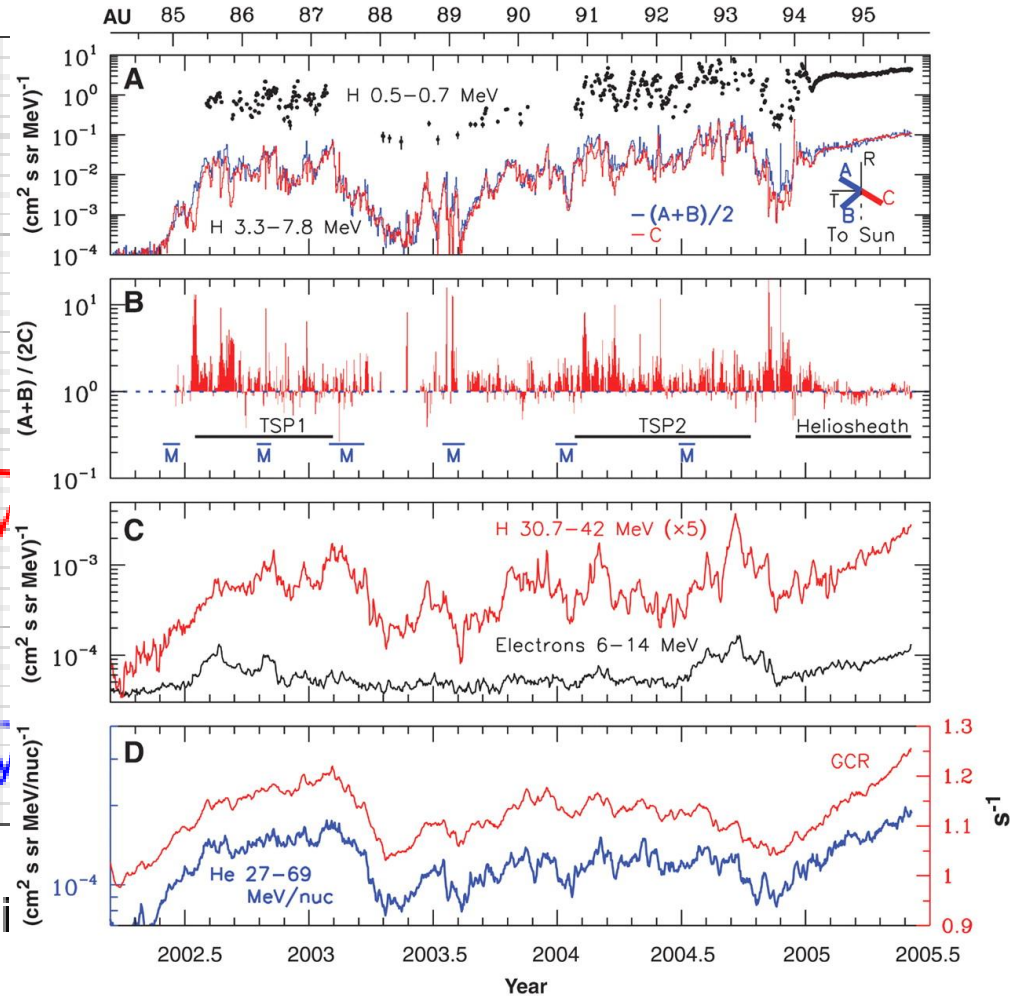
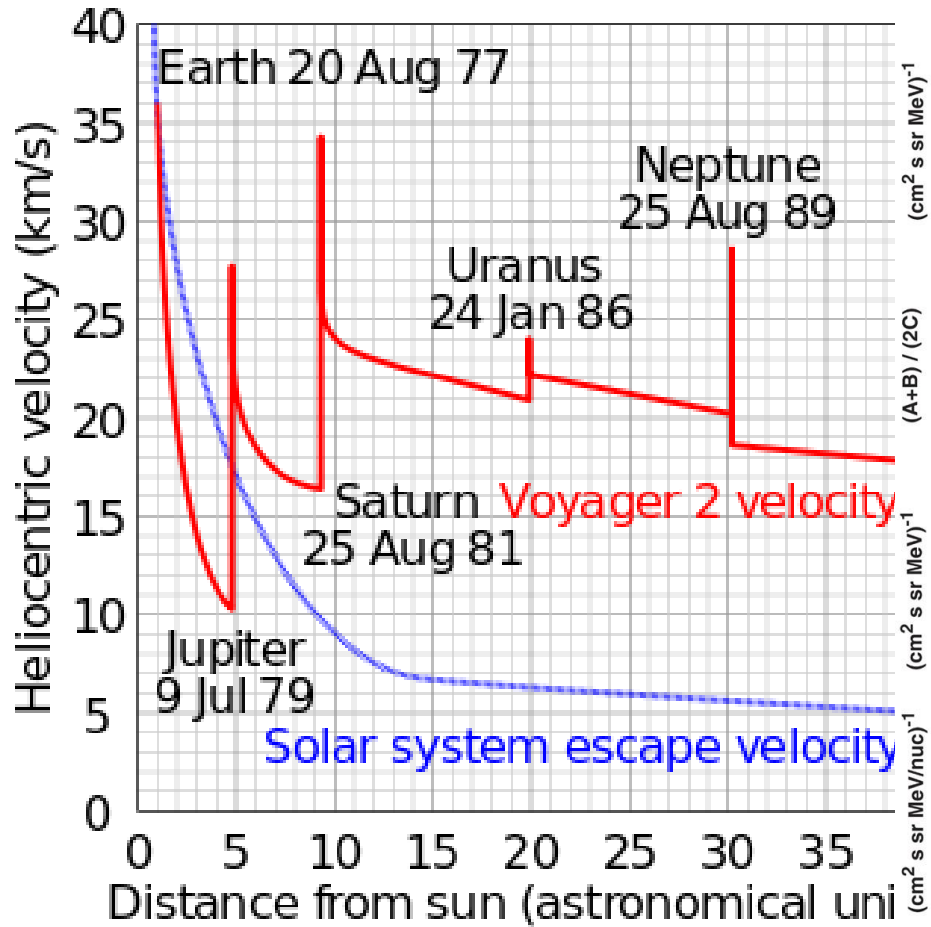
Voyager 2

← Termination Shock

← Heliopause

Heliosphere

# Voyager 2





# The latest from Voyager 2

THE ASTROPHYSICAL JOURNAL, 818:147 (16pp), 2016 February 20

doi:10.3847/0004-637X/818/2/147

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## HELIOSHEATH MAGNETIC FIELD AND PLASMA OBSERVED BY VOYAGER 2 DURING 2012 IN THE RISING PHASE OF SOLAR CYCLE 24

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<sup>4</sup>Johns Hopkins University, Applied Physics Laboratory, Laurel, Maryland, USA

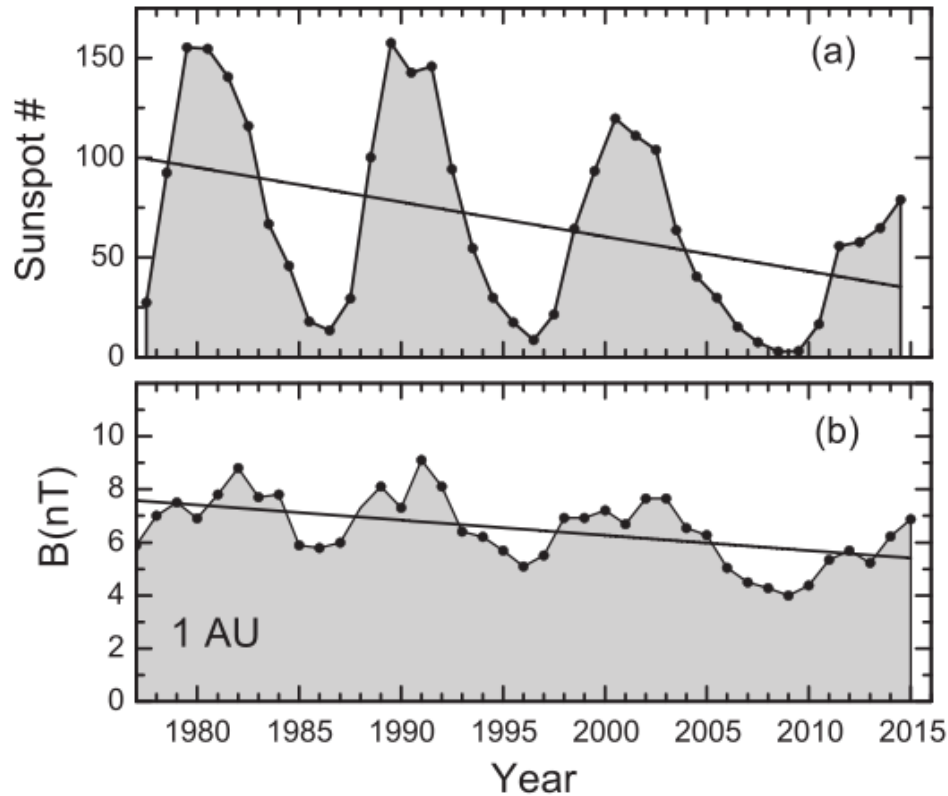
Received 2015 October 22; accepted 2016 January 5; published 2016 February 17

### ABSTRACT

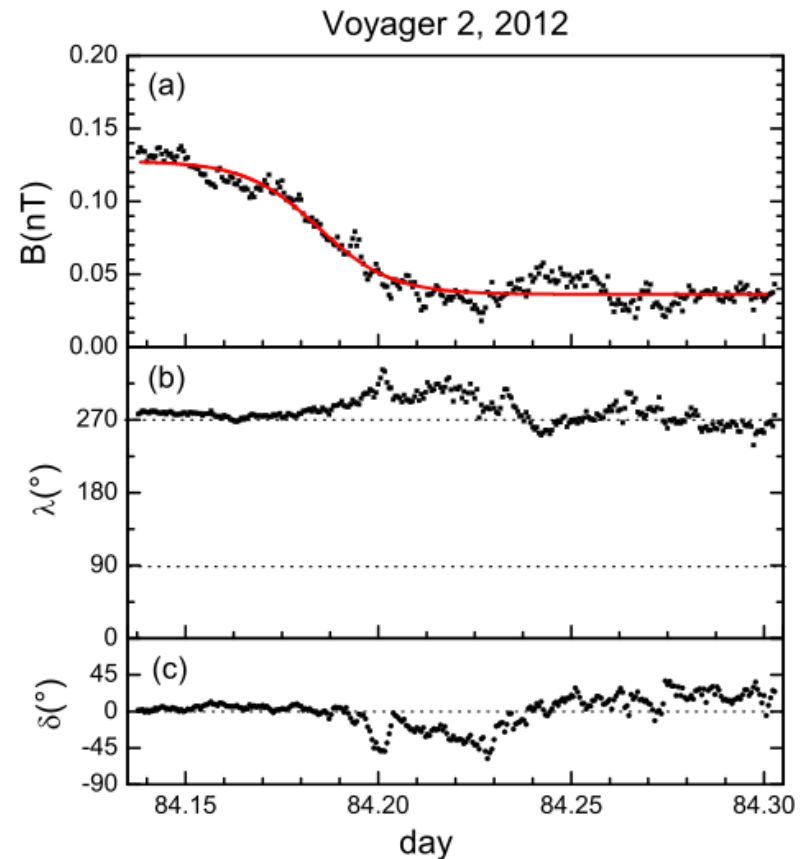
We discuss magnetic field and plasma observations of the heliosheath made by *Voyager 2* (V2) during 2012, when V2 was observing the effects of increasing solar activity following the solar minimum in 2009. The average magnetic field strength  $B$  was 0.14 nT and  $B$  reached 0.29 nT on day 249. V2 was in a unipolar region in which the magnetic polarity was directed away from the Sun along the Parker spiral 88% of the time, indicating that V2 was poleward of the heliospheric current sheet throughout most of 2012. The magnetic flux at V2 during 2012 was constant. A merged interaction region (MIR) was observed, and the flow speed increased as the MIR moved past V2. The MIR caused a decrease in the  $>70$  MeV  $\text{nuc}^{-1}$  cosmic-ray intensity. The increments of  $B$  can be described by a  $q$ -Gaussian distribution with  $q = 1.2 \pm 0.1$  for daily averages and  $q = 1.82 \pm 0.03$  for hour averages. Eight isolated current sheets (“PBLs”) and four closely spaced pairs of current sheets were observed. The average change of  $B$  across the current sheets was a factor of  $\approx 2$ , and  $B$  increased or decreased with equal probability. Magnetic holes and magnetic humps were also observed. The characteristic size of the PBLs was  $\approx 6 R_L$ , where  $R_L$  is the Larmor radius of protons, and the characteristic sizes of the magnetic holes and humps were  $\approx 38 R_L$  and  $\approx 11 R_L$ , respectively.

*Key words:* magnetic fields – plasmas – Sun: heliosphere

# Voyager 2



**Figure 3.** Yearly averages of (a) the sunspot number and (b) magnetic field strength observed at 1 au show the tendency for solar activity to decrease from 1977 to 2015 and the corresponding tendency for  $B$  at 1 au to decrease. The solar activity and  $B$  reached a minimum at 1 au during 2009 and they have been increasing since 2010. It takes approximately one year for the magnetic fields and plasma observed at 1 au to reach V2 during 2012.



**Figure 11.** Proton boundary layer across which (a)  $B$  decreased and there was little or no net change across in (b) the angle  $\lambda$  or (c) the angle  $\delta$ . The data points are 48 s averages of  $B$ .

# *How far is Voyager 1 now?*

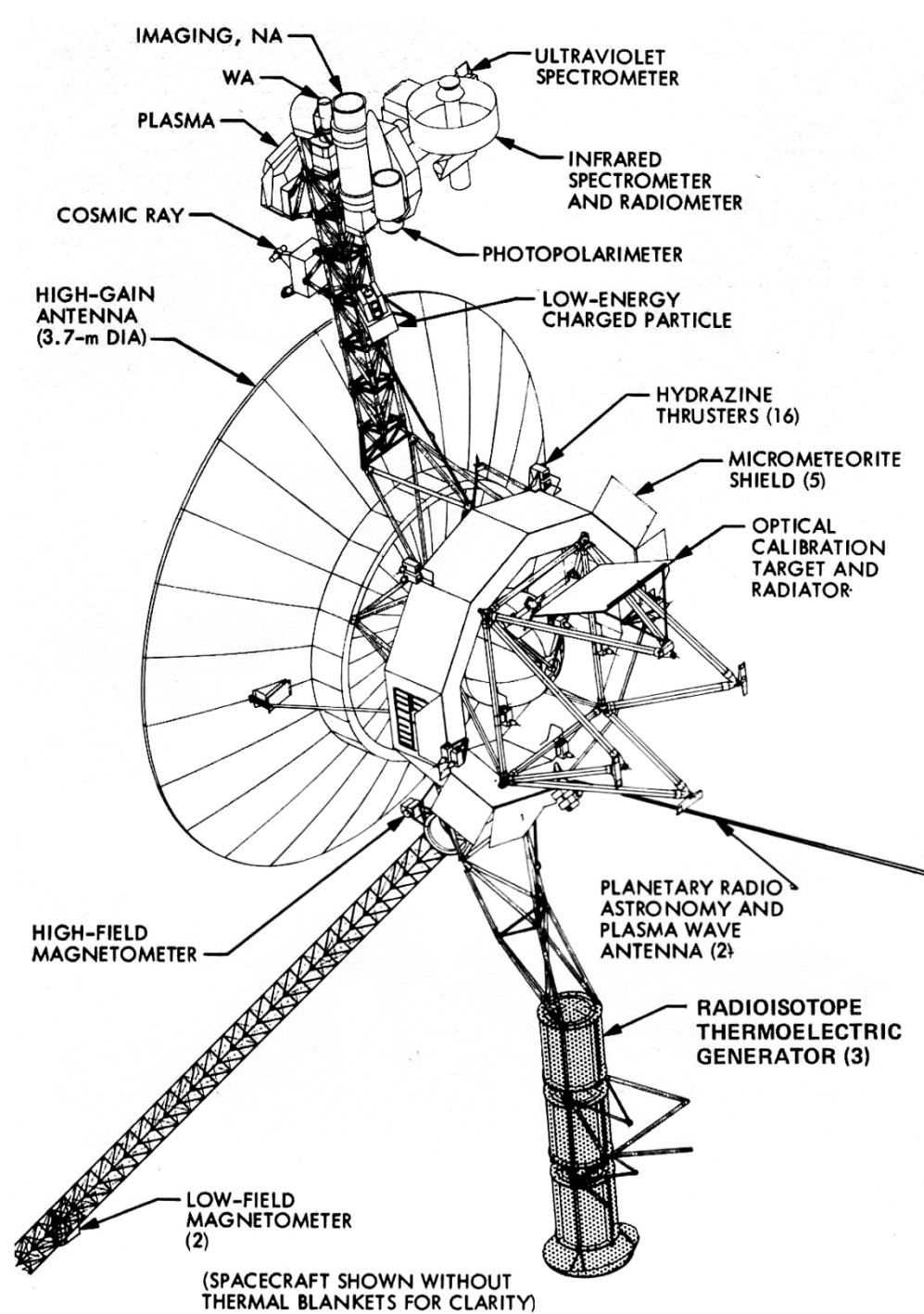
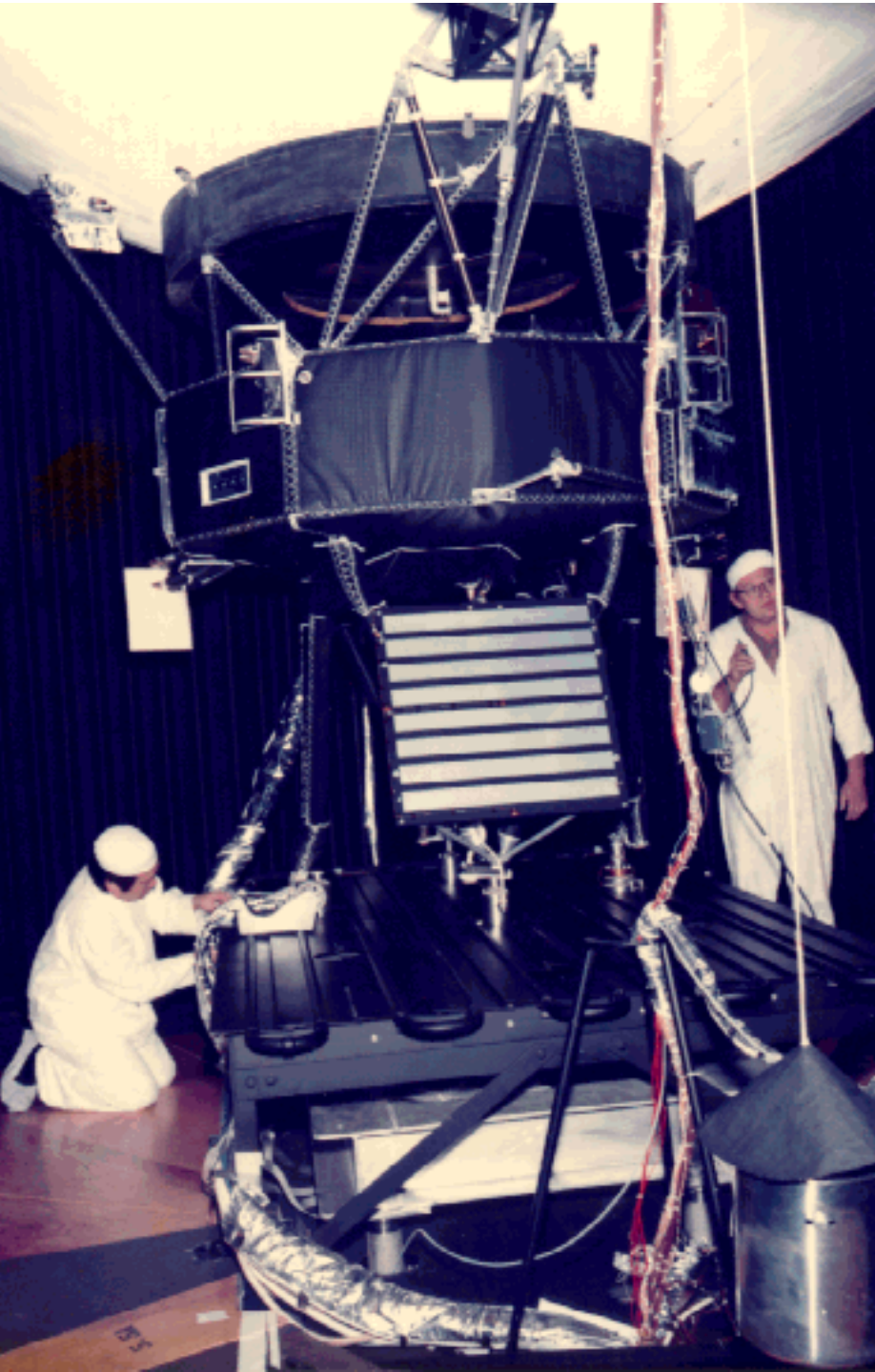
- A. 62 AU
- B. 76 AU
- C. 82 AU
- D. 134 AU
- E. 153 AU

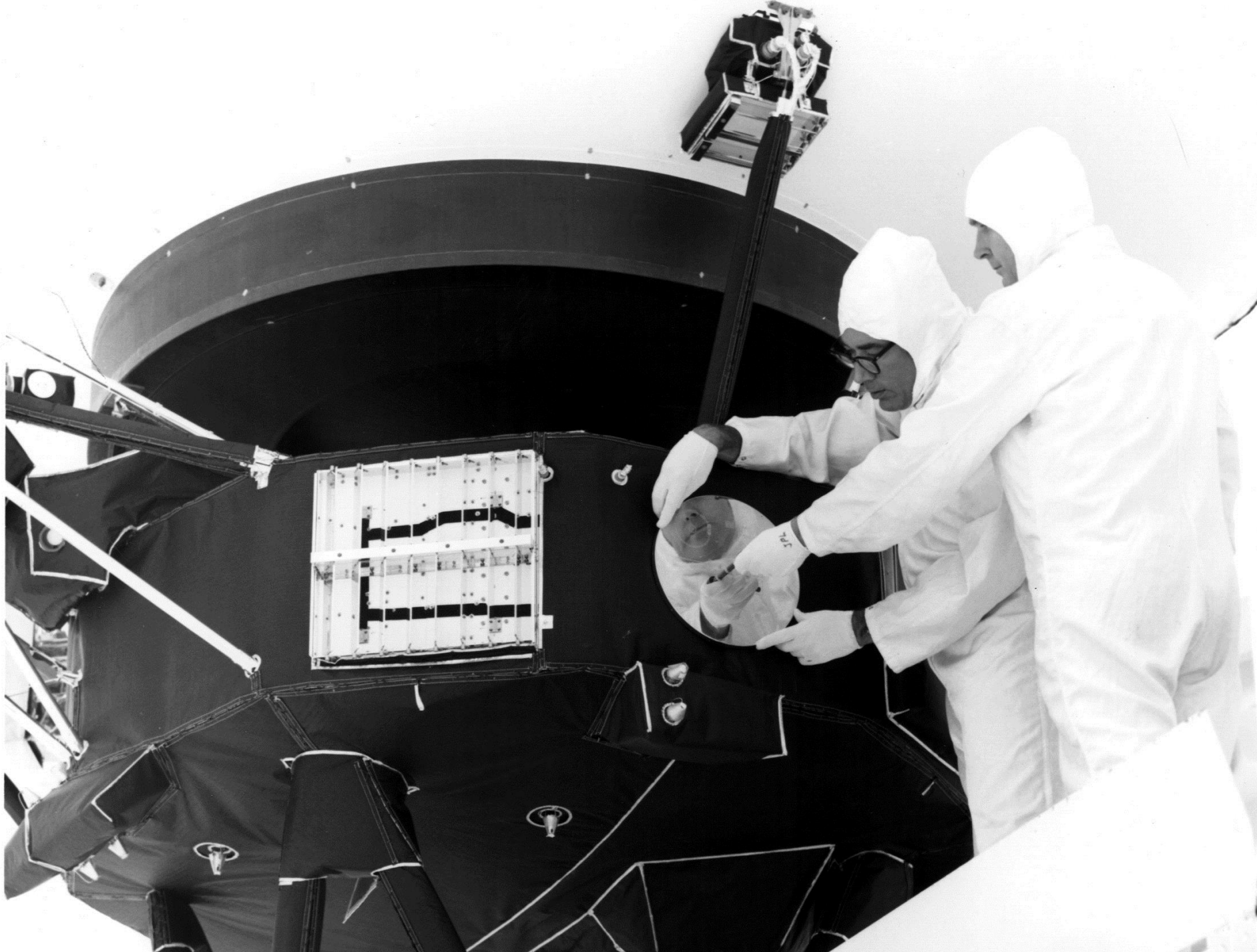
# *When was it launched*

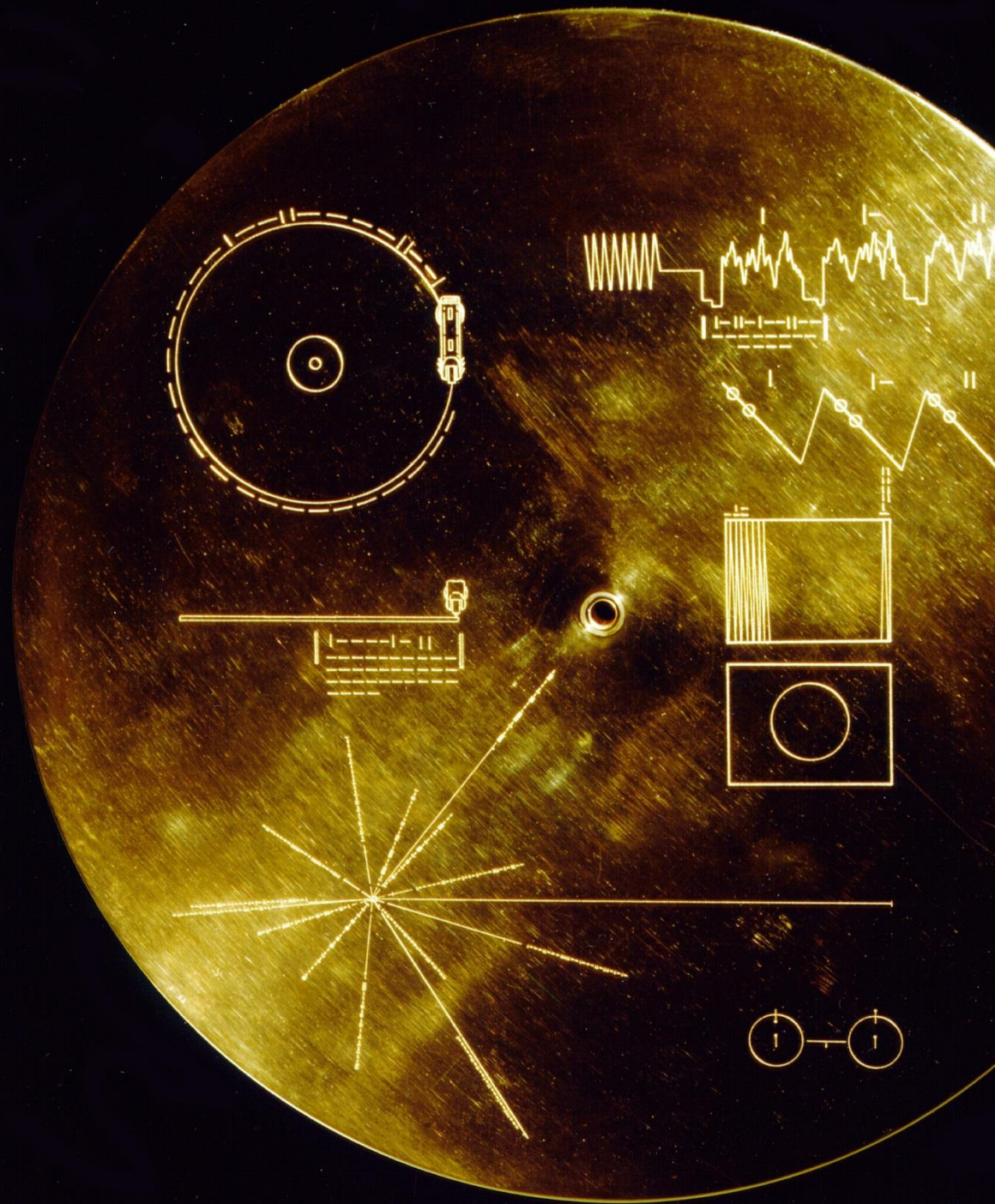
- A. 1967
- B. 1977
- C. 1987
- D. 1997
- E. 2007

# *Voyager 1+2*

- Voyager 1: Sept 5, 1977
  - Most distant (134 AU, 37 lh/2)
  - North (Saturn in 1980)
  - Nuclear batteries until 2020
- Voyager 2
  - Jupiter, Saturn, Uranus, Neptune!
  - South (Uranus in 1986)
  - 110 AU, 15 km/s





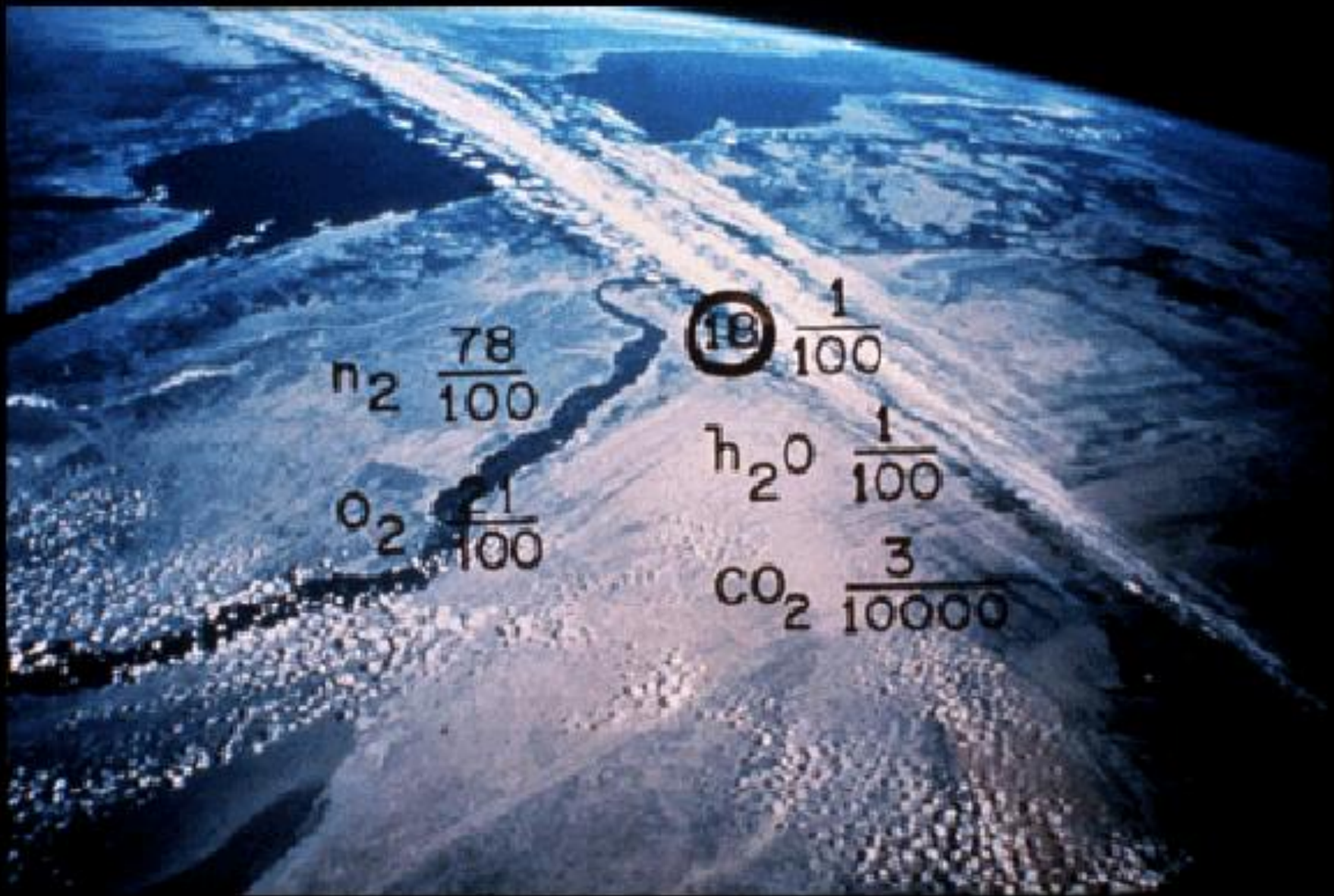






142800 km  
318 e

11/10/01



$N_2 \frac{78}{100}$

$O_2 \frac{1}{100}$

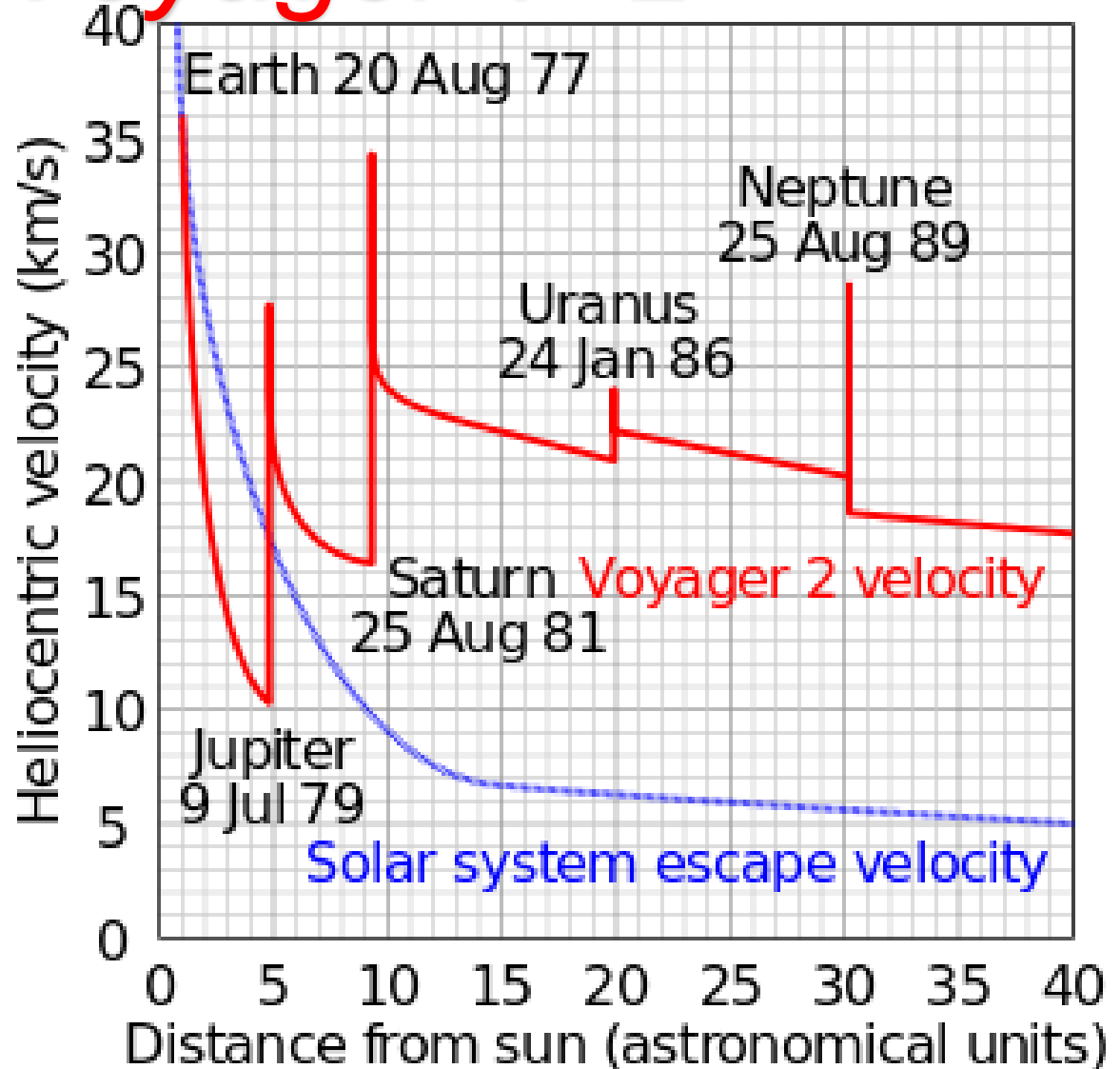
**Ar**  $\frac{1}{100}$

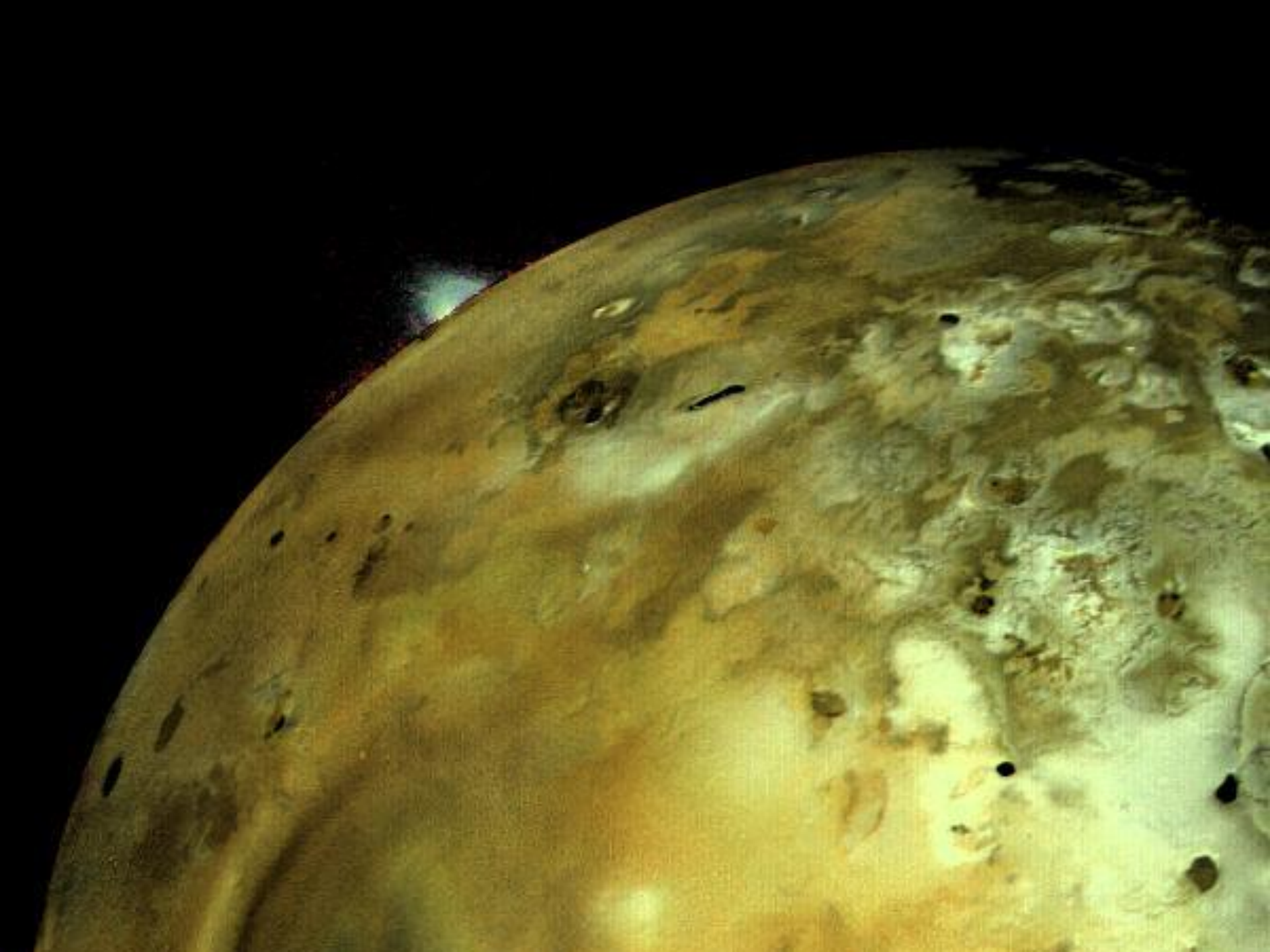
$H_2O \frac{1}{100}$

$CO_2 \frac{3}{100000}$



# Voyager 1+2





# THE GENERATION OF NONAXISYMMETRIC MAGNETIC FIELDS IN THE GIANT PLANETS

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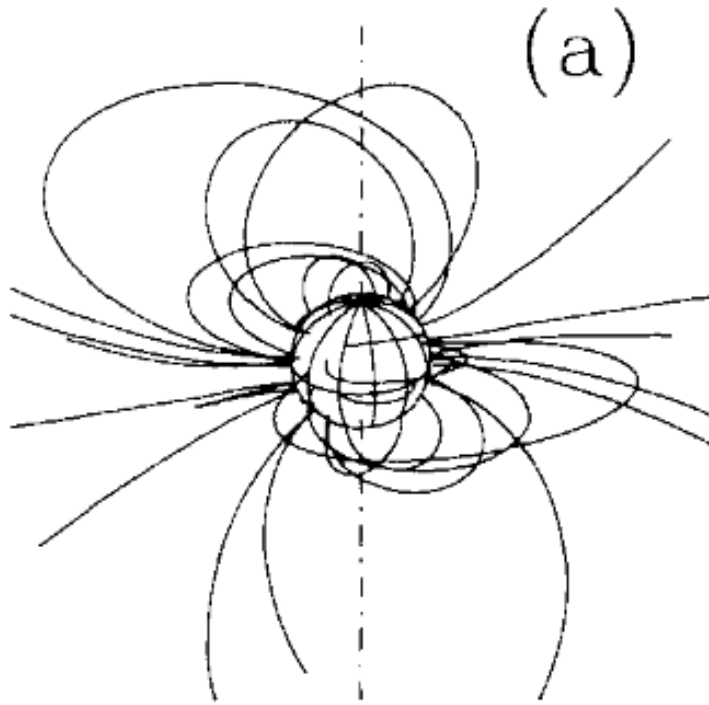
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National Center for Atmospheric Research<sup>†</sup>,  
P.O. Box 3000, Boulder, CO 80307-3000, USA*

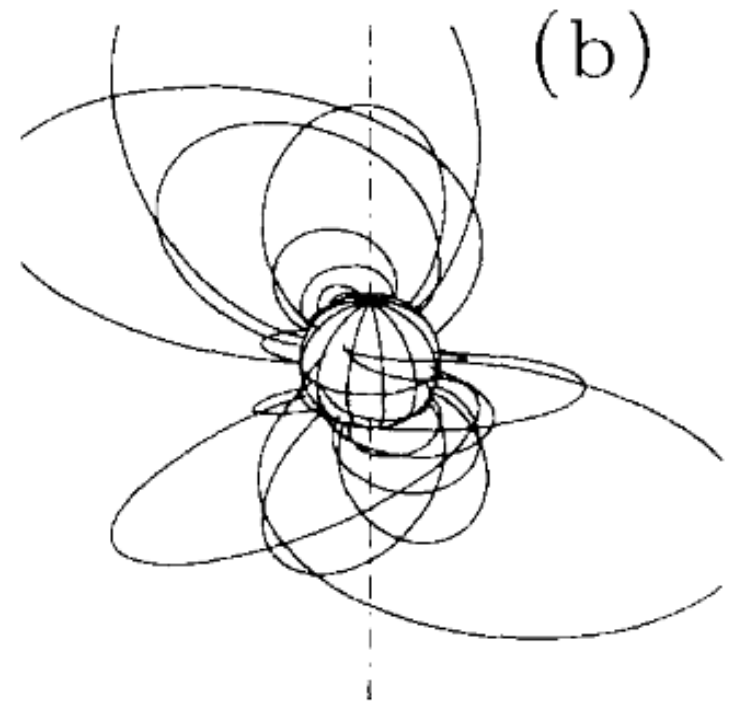
*(Received 2 February 1995; in final form 4 May 1995)*

## 1. INTRODUCTION

The dipole moments of the magnetic fields of Jupiter and Saturn are quite closely aligned with the rotation axes, in contrast to the magnetic fields of Uranus and Neptune which are highly nonaxisymmetric with dipole moments almost perpendicular to the rotation axes. The origin of this difference is very puzzling. Possible explanations include that Uranus and Neptune just happen to be in a state of field reversal, similar to the reversals found in geological records of the earth's magnetic field (Schultz and Paulikas, 1990; Rädler and Ness, 1990), or that the types of dynamos that operate in Uranus and Neptune are fundamentally different from those of Jupiter and Saturn (Connerney *et al.*, 1991), in that the fields of Uranus and Neptune are generated close to the surfaces of these planets, whereas the fields of Jupiter and Saturn are generated in deeper layers. For example, Stevenson (1982) proposed that the very high



Uranus & Neptune  
(less differential rotation)



Jupiter & Saturn  
(more differential rotation)

We thank Günther Rüdiger for pointing out the need for these investigations, and Fran Bagenal, Paul Charbonneau, John Hart, and Michel Rieutord for discussions and further references concerning the physics of the outer planets.

### *References*

Bagenal, F., "Giant planet magnetospheres," *Annu. Rev. Earth Planet. Sci.* **20**, 289–328 (1992).

# *What we learned today*

- Solar wind turbulence
  - Energy spectrum
  - Dimensional analysis
- Heliosphere & termination shock
- Voyager 1 + 2
  - Messages to us & from us
  - Magnetic fields of planets