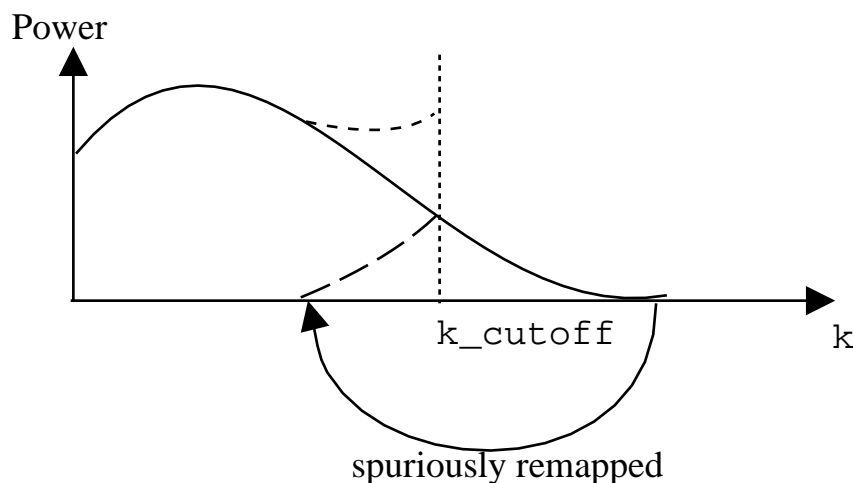


PARALLEL CODE: DEALIASING

If the signal to be Fourier-transformed is band-width-limited, and you use a discrete transform that encompasses the band, then the result is exact.

If the signal had power outside the range of the transform, then the missing frequencies are **ALIASED** back into the range of the transform.



k_{cutoff} --- max retained frequency

Nonlinear interactions produce frequencies up to --- $2*k_{\text{cutoff}}$

Spurious frequencies folded back --- k_{cutoff} maps to itself
 $2*k_{\text{cutoff}}$ maps to zero

$(k_{\text{cutoff}}+k)$ maps to $(k_{\text{cutoff}}-k)$

$k_{\text{dealias}} = 2/3*k_{\text{cutoff}}$

Zero out all $k > k_{\text{dealias}}$

Now nonlinear terms produce k 's up to $2*k_{\text{dealias}} = 4/3*k_{\text{cutoff}}$

$[k_{\text{cutoff}}:(4/3*k_{\text{cutoff}})]$ is aliased into $[2/3*k_{\text{cutoff}}:k_{\text{cutoff}}]$

and we are **ZEROING** out this bit!

i.e. if we only keep the first 2/3 of the frequencies, they remain **UNCONTAMINATED** by aliasing errors.

BIG ADVANTAGE:

If we only keep the wavenumbers up to k_{dealias} , then we save 1/3 of the memory and the communication.

*In 2D, we are doing only $2/3*2/3 = 4/9 < 1/2$ of the work!*