

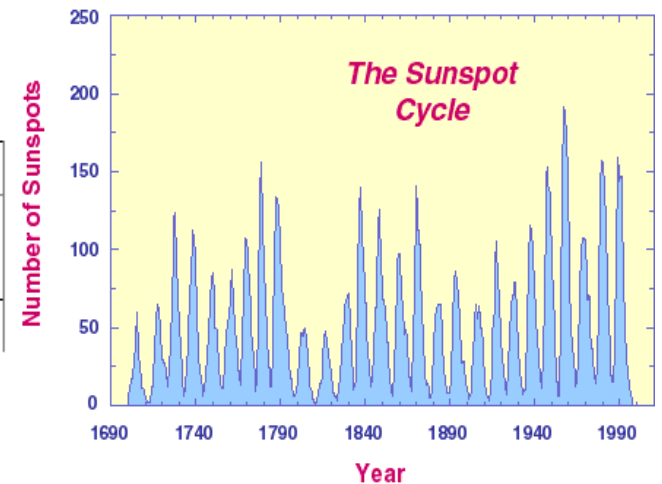
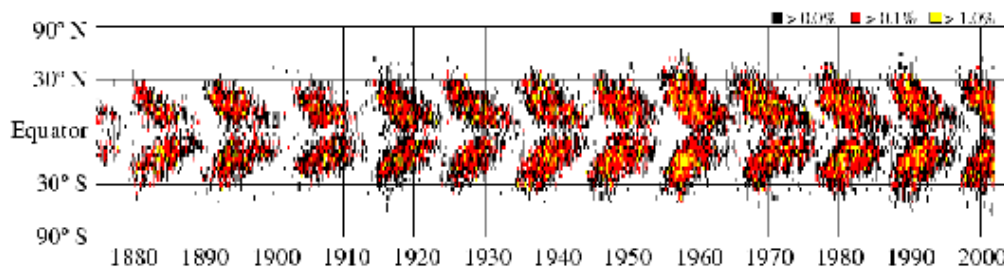
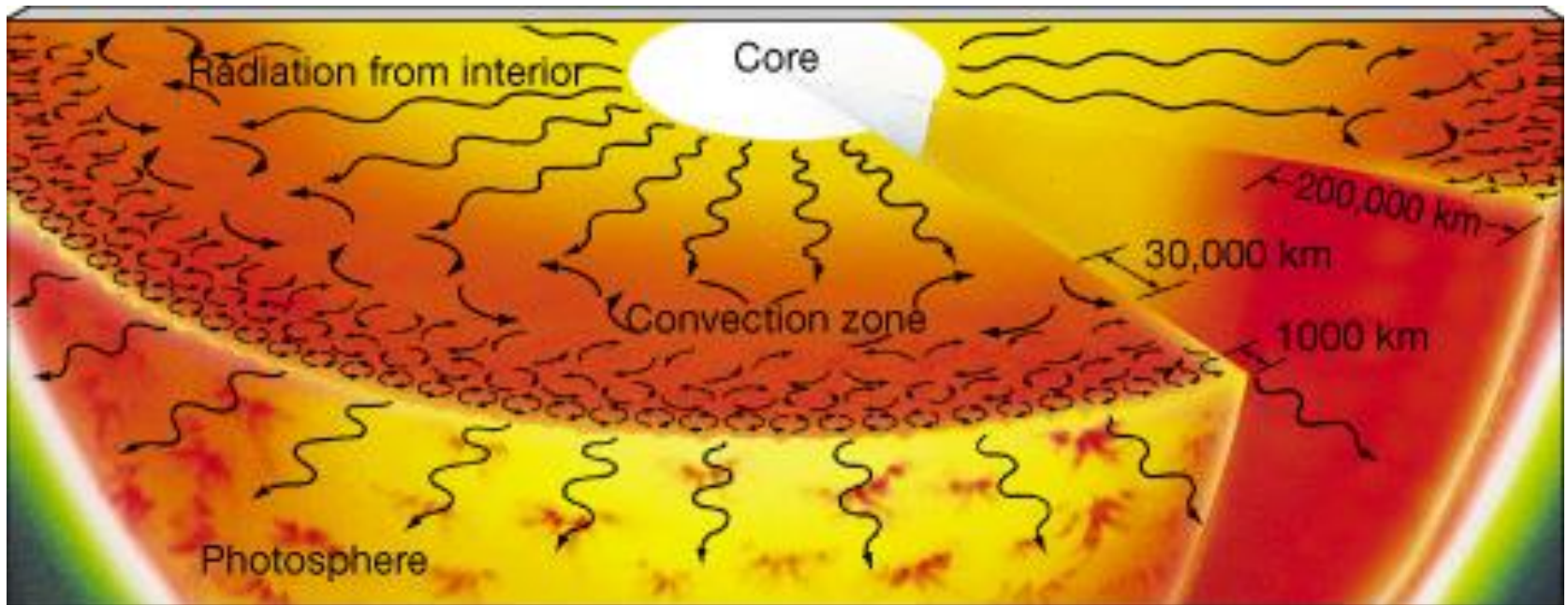
# *Lecture 17*

- Solar cycle
- Induction equation
- Conversion between kinetic and magnetic energy forms
- Alfven waves (beginning)

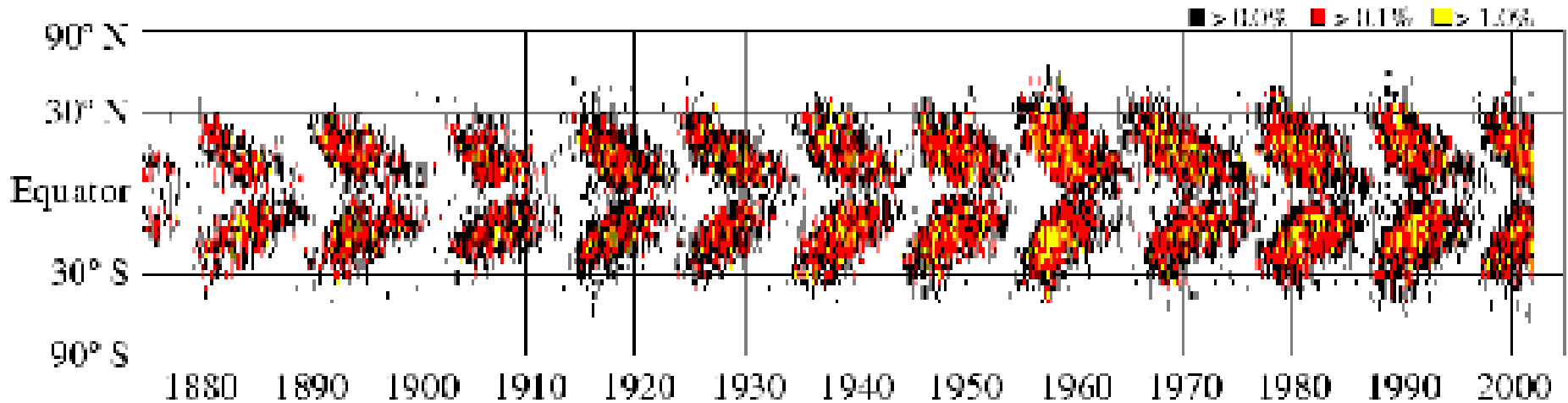
# *Last time*

- Center to limb variation, HW2
- Entropy: what makes it change
- Buoyancy oscillations
- Energy equation

# *The solar cycle*



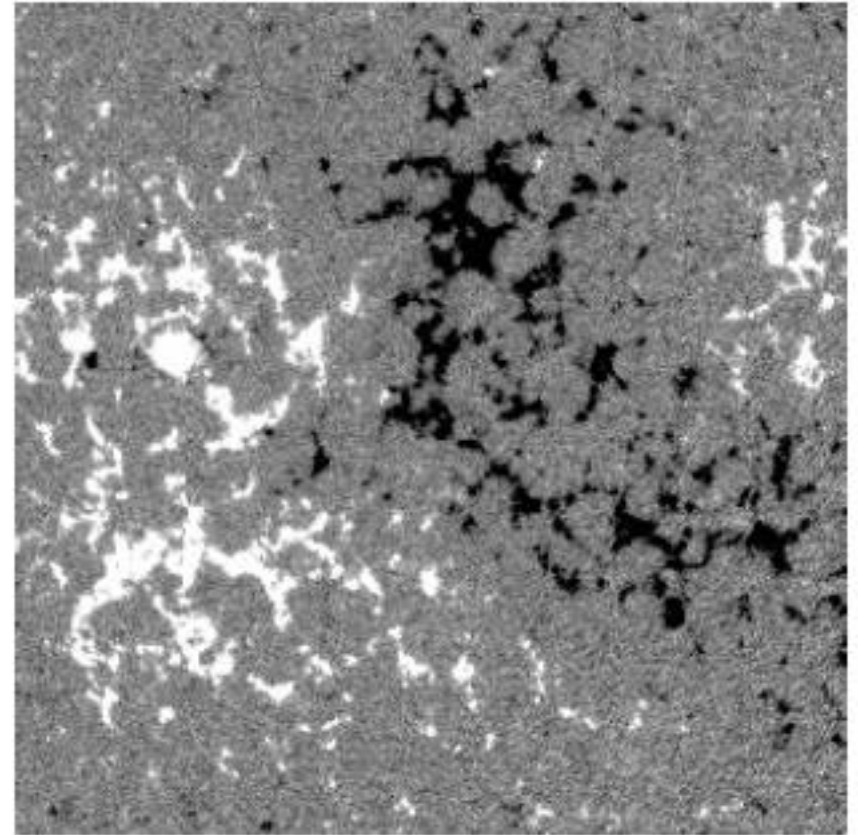
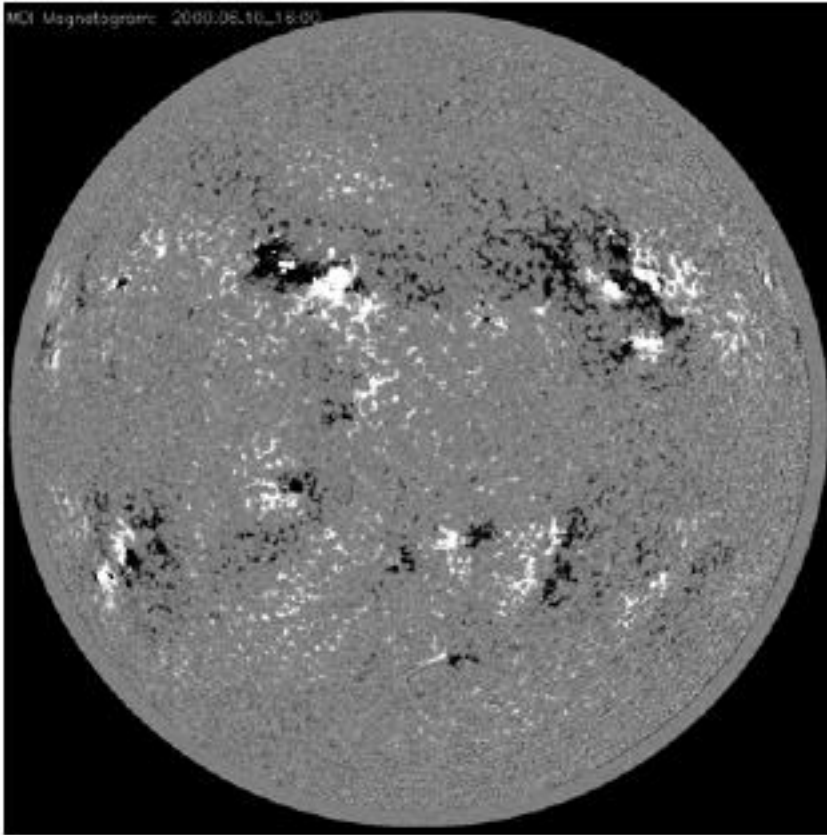
# Solar 11 year sunspot cycle



butterfly diagram

- Sunspots between +/- 30 degrees around equator
- New cycle begins at high latitude
- Ends at low latitudes
  - equatorward migration

# Large scale coherence

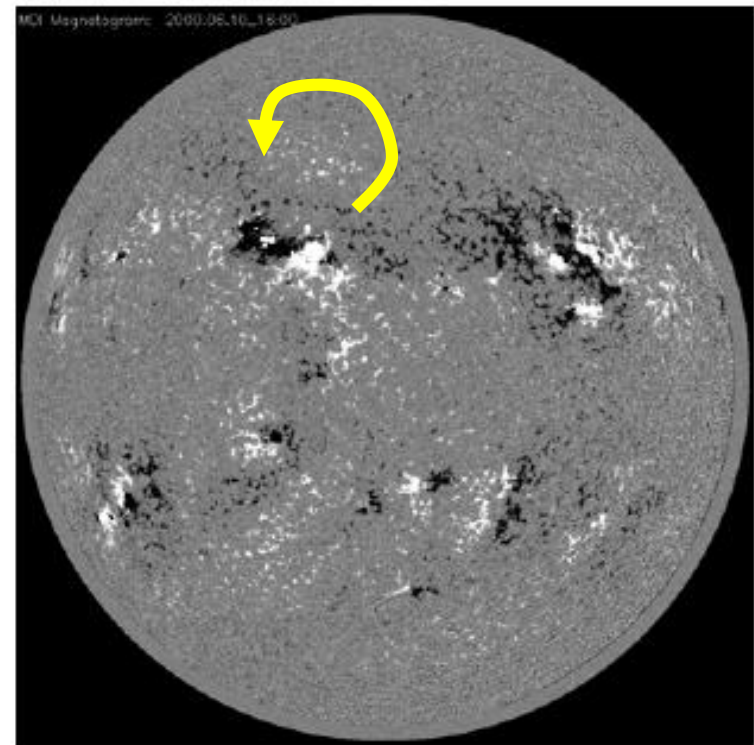


Active regions, bi-polarity  
systematic east-west orientation  
opposite in the south

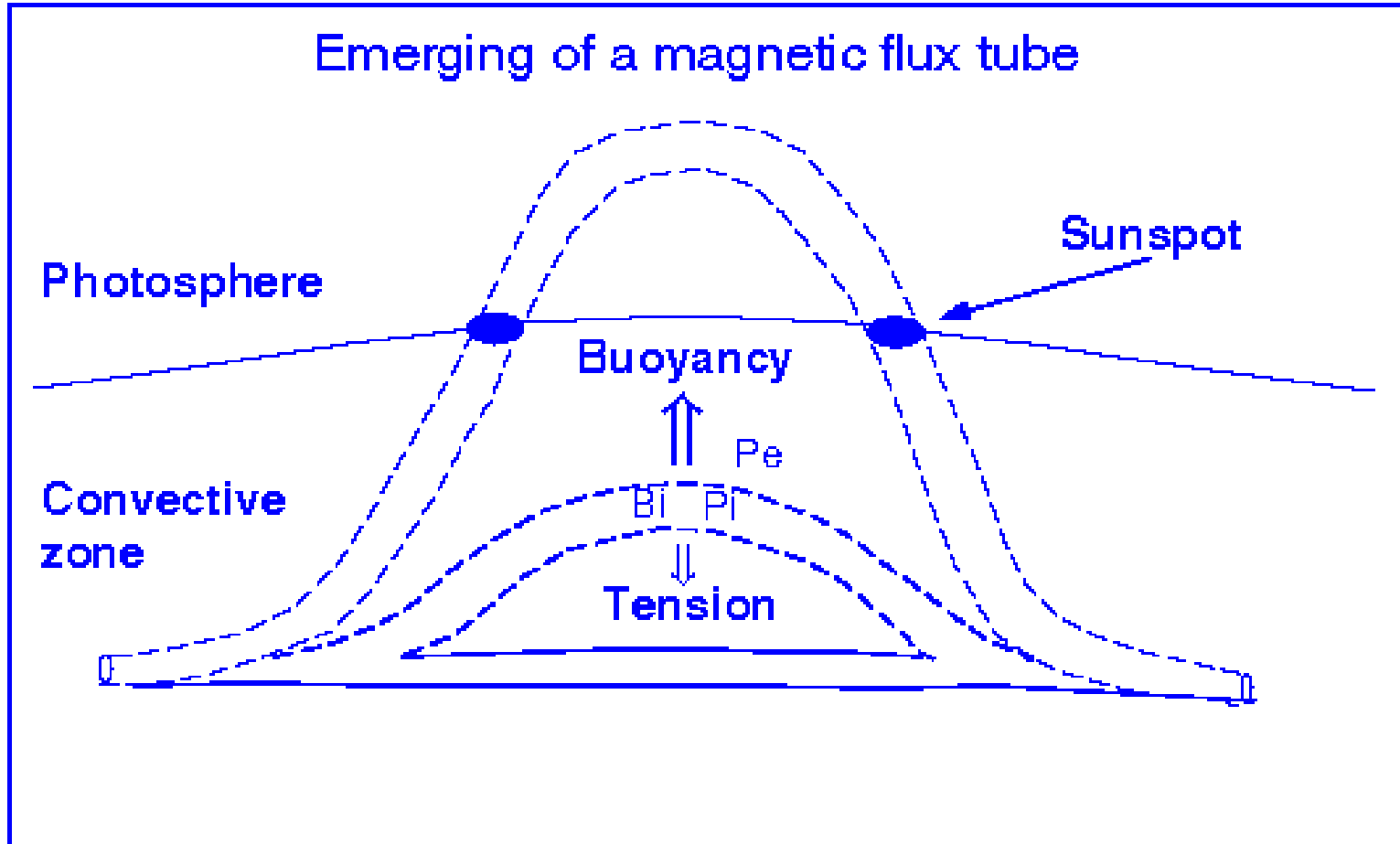
# The Sun today and 9 years ago



Solar magnetograms:  
Line of sight B-field from  
circularly polarized light



# Buoyant rise of flux tubes



*Is charge accelerated by  
B field*

- A. Yes
- B. No



*Is charge accelerated by  
E field*

- A. Yes
- B. No

Assuming that the relative velocity  $v$  is much smaller than the speed of light, we analyze the Lorentz force on the charged particle (as measured in both frames) as follows:

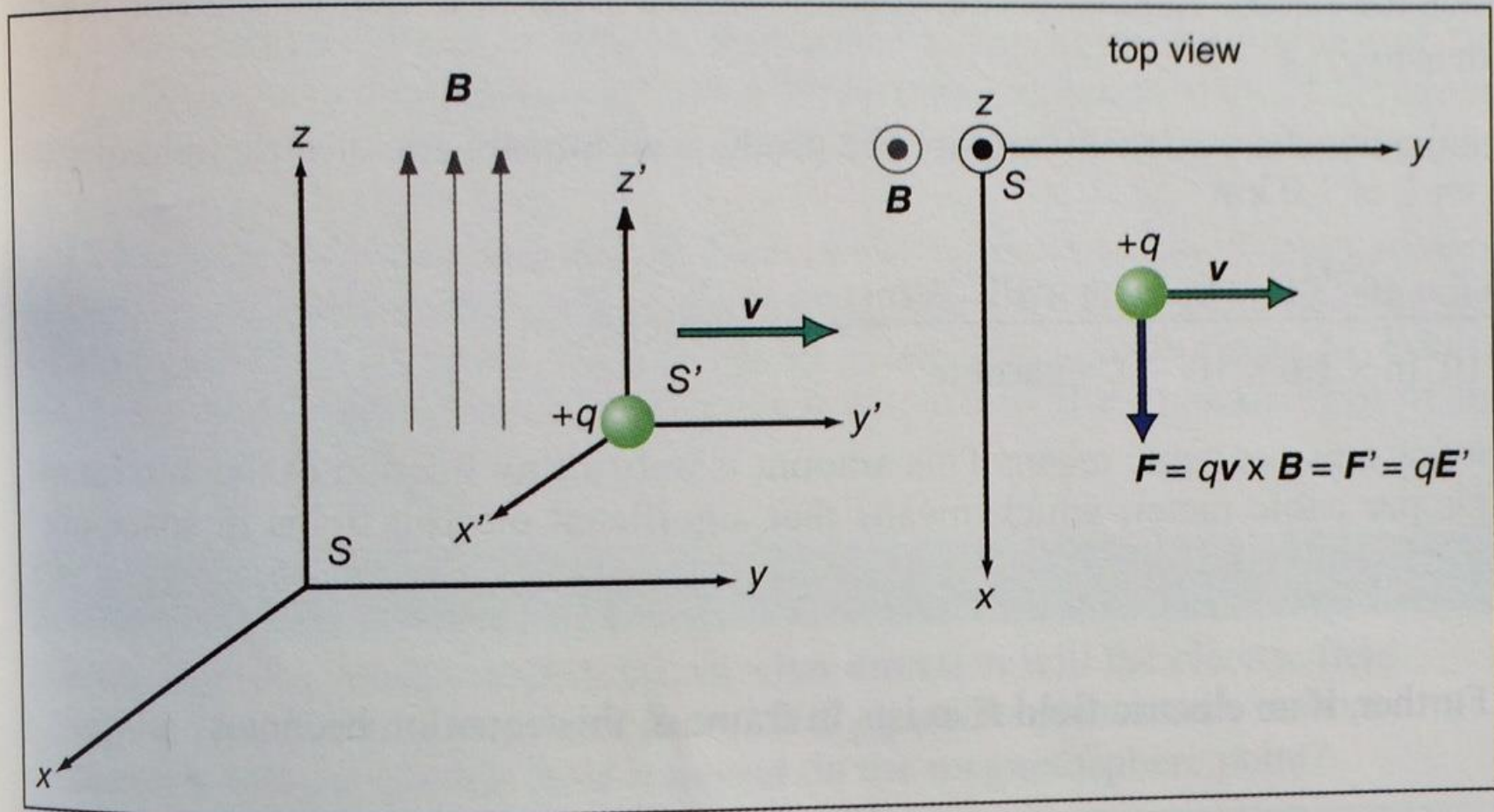


Fig. 4  
as  $V$   
left pa  
veloci  
field, p  
 $z$ -axis  
a top-  
charge  
charge  
mome  
force  
frame  
unprin  
refere

Suppose the particle is initially restrained by the observer in  $S'$ , and then released. Because both observers are in inertial frames, they must agree on the magnitude and direction of the force vector acting on the charged particle at the moment it is released. However, the two observers will disagree on the cause of

## *Lab (S) and comoving (S') frames*

Observer in S sees charge moving

$$\mathbf{F} = q\mathbf{u} \times \mathbf{B}$$

Observer in S' sees charge moving sideways

$$\mathbf{F}' = q\mathbf{E}'$$

Therefore, because  $F=F'$ ,

$$\mathbf{E}' = \mathbf{u} \times \mathbf{B}$$

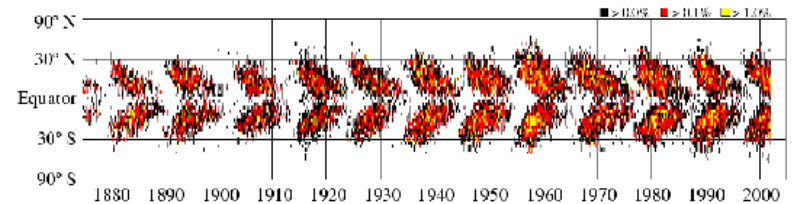
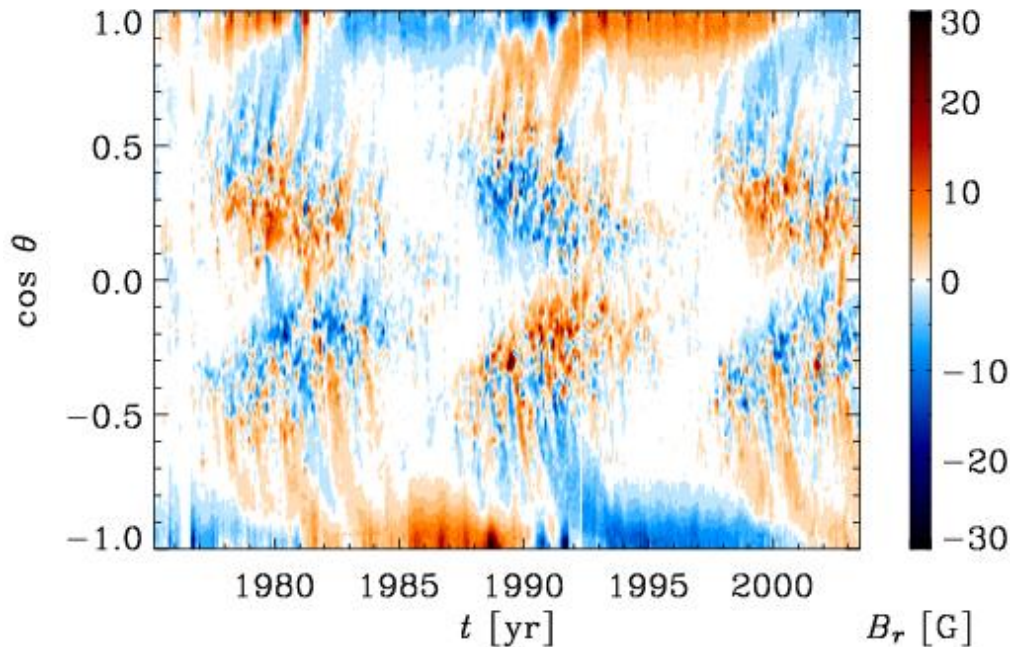
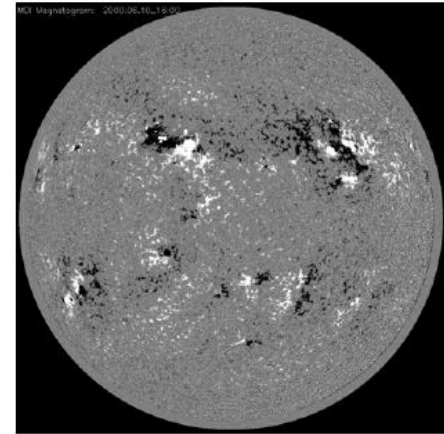
*If additional background field*

Therefore

$$\mathbf{E}' = \mathbf{E} + \mathbf{u} \times \mathbf{B}$$

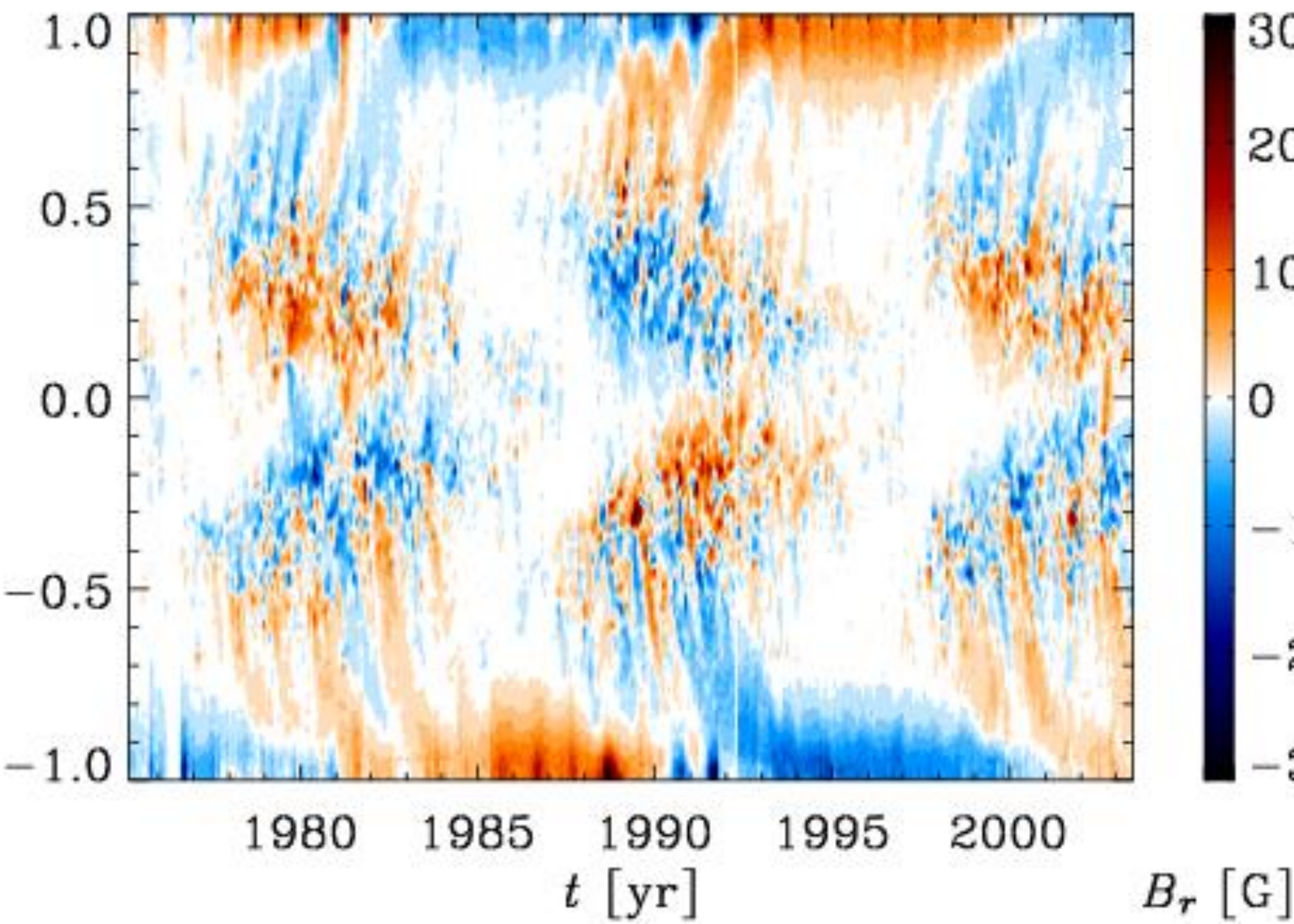
# 22 year magnetic cycle

- Longitudinally averaged radial field
- Spatio-temporal coherence
  - 22 yr cycle, equatorward migration

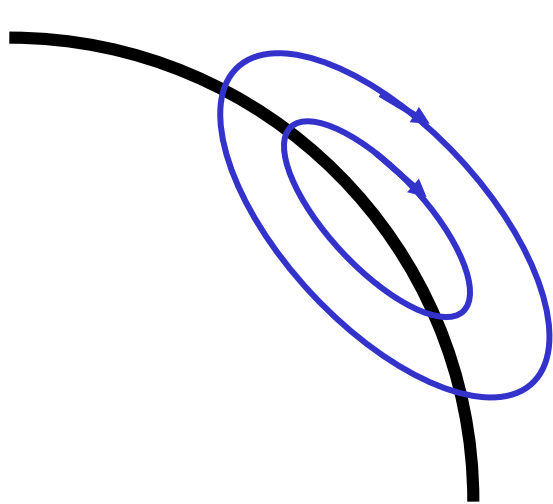


butterfly diagram

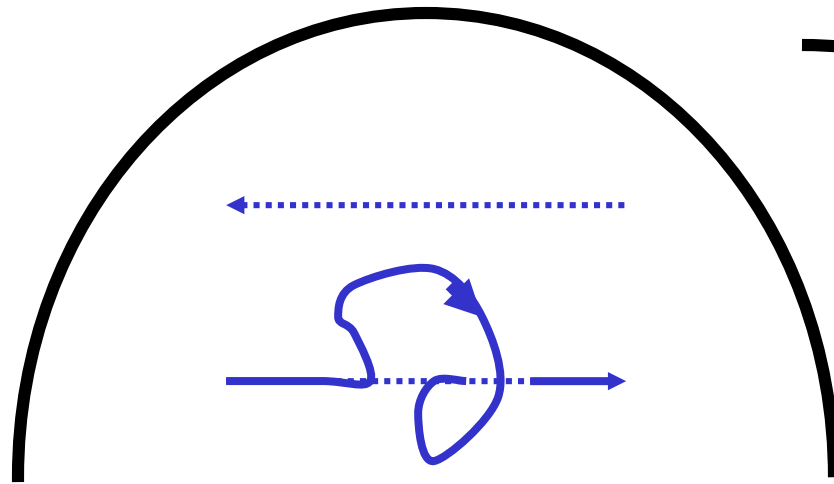
Poleward branch or  
poleward drift?



# $\alpha$ -effect dynamos (large scale)

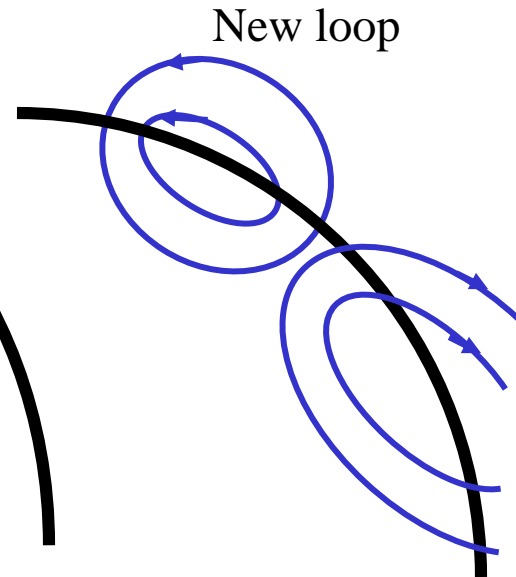
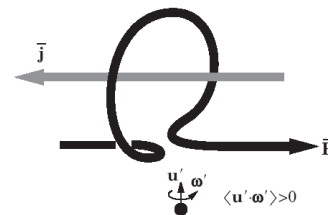


Differential rotation  
(faster inside)

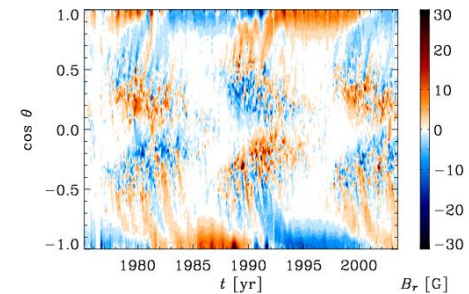
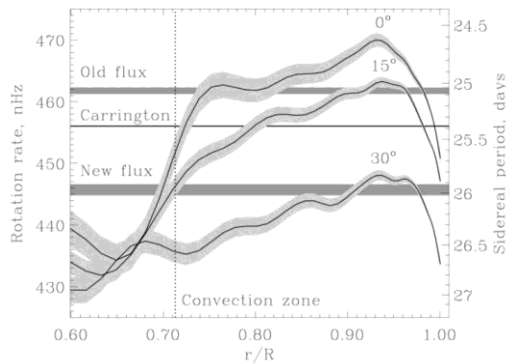


Cyclonic convection;  
Buoyant flux tubes

$\rightarrow$   $\alpha$ -effect



Equatorward  
migration



# *What we learned*

- Conversion of kinetic into magnetic energy
- How magnetic fields get advected